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Christopher Gust

Nathan Sheets

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# The Adjustment of Global External Balances: Does Partial Exchange Rate Pass-Through to Trade Prices Matter?\*

Christopher Gust and Nathan Sheets<sup>†</sup>

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## Abstract

This paper assesses whether partial exchange rate pass-through to trade prices has important implications for the prospective adjustment of global external imbalances. To address this question, we develop an open-economy DGE model in which firms set their prices with an eye toward maintaining their competitiveness against other producers; this feature of the model generates a variable desired markup and, hence, pass-through that is less than complete. With trade price elasticities of unity or greater, we find that for a given move in the exchange rate the nominal trade balance adjusts more when pass-through is high. However, an offsetting consideration is that the exchange rate tends to be more sensitive to shocks in a low pass-through environment. We show that the relative importance of these considerations depends on the structural features of the economy, including the magnitude of the trade price elasticities and the sensitivity of private spending to shocks.

Keywords: Import prices, Export prices, Trade balance, Marshall-Lerner condition, DGE model

JEL classification: F3, F41

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<sup>†</sup>Corresponding Author: Christopher Gust, Address: Federal Reserve Board, Mail Stop 42, Washington DC, 20551, Telephone: 202-452-2383, Fax: 202-872-4926. Email addresses: christopher.gust@frb.gov and nathan.sheets@frb.gov.

# 1 Introduction

Research over the past several decades has unearthed compelling empirical evidence that exchange rate pass-through to U.S. import prices is well below unity.<sup>1</sup> That is, foreign exporters typically do not adjust the dollar-price that they charge in the U.S. market one-for-one in response to moves in the exchange rate but, instead, absorb a portion of the exchange rate change into their (home-currency denominated) profit margins.

Much of the previous work examining partial exchange rate pass-through to trade prices has emphasized the implications for monetary policy and for domestic inflation.<sup>2</sup> Our contribution is to examine an additional channel through which partial pass-through might affect economic performance at home and abroad—that is, by influencing the features of global external adjustment. Such considerations have loomed increasingly large as the U.S. current account deficit has widened significantly in recent years, with rising counterpart surpluses elsewhere in the world.

We tackle this issue using an open-economy, dynamic general equilibrium (DGE) model. A central methodological feature of this model is that firms face a non-constant elasticity of demand, as in Dotsey and King (2005) and Gust, Leduc, and Vigfusson (2006). As a result, firms set their prices with an eye toward maintaining their competitiveness against other producers, and it is optimal for firms to vary their markups. This mutes the responsiveness of export prices following shocks that otherwise would have prompted exporting firms to raise their prices above those of their competitors. This feature of the model gives rise to incomplete pass-through, even in the absence of nominal rigidities.

In the course of our work, we consider how changes in pass-through affect the trade balance when domestic and foreign activity are held constant and the exchange rate is treated as exoge-

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<sup>1</sup> For example, Goldberg and Knetter (1997) in their extensive survey of the empirical literature found that estimates of exchange rate pass-through to U.S. import prices were at that time centered near 0.5, meaning that a 10 percent depreciation of the dollar was typically associated with a 5 percent rise in U.S. import prices. More recent evidence, such as that put forward by Marazzi, Sheets, and Vigfusson (2005), suggests that exchange rate pass-through to U.S. import prices may have fallen well below those earlier estimates.

<sup>2</sup> See, for example, Corsetti and Pesenti (2005) and Devereux and Engel (2003), who show how optimal monetary policy depends on the extent of exchange rate pass-through.

nous (partial equilibrium) and when these variables are allowed to vary (general equilibrium). We emphasize the case in which trade-price elasticities are roughly unity, in accordance with our interpretation of the macro data, but we consider other possibilities as well. We focus particularly on the nominal trade balance because, for reasons discussed below, we see this as the central barometer of external adjustment.

*Partial-Equilibrium Results:* When trade-price elasticities are near unity, a one-percent depreciation of the exchange rate improves the trade balance by one percent of the value of exports, regardless of the extent of pass-through. The intuition for this result is as follows:

- Spending on imports is unchanged, as any rise in import prices is exactly offset by a decline in import volumes.
- Export revenues rise by one percent. Foreign spending on home exports is unchanged in terms of the foreign currency, but the value of these expenditures expressed in terms of the home currency increases one-for-one with the exchange rate. If import price pass-through abroad is zero, all of this increase comes from a rise in home-currency denominated export prices (with quantities unchanged); if pass-through is complete, it all comes from a rise in export volumes (with home-currency export prices unchanged).

*General-Equilibrium Results:* In our general equilibrium analysis, monetary policy is assumed to follow a Taylor rule at home and abroad, and we consider a variety of shocks that induce exchange rate changes. In this richer framework, we identify two broadly offsetting effects that are at work:

- First, a decline in pass-through tends to mute the sensitivity of the real economy to a change in the exchange rate, damping the general-equilibrium feedback effects that attend the exchange rate move, thus limiting the adjustment of the nominal trade balance. In particular, when pass-through is low, absorption (and, hence, import demand) is less affected by a given move in the exchange rate.
- Second, consistent with this observation, with low pass-through the depreciation of the home currency puts less upward pressure on domestic prices and output and, accordingly, leads to a smaller rise in domestic interest rates. For this reason, the decline in the exchange rate is relatively large when pass-through is low, which has the effect of inducing greater nominal trade adjustment, if all else is equal.<sup>3</sup>

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<sup>3</sup> As discussed in Devereux and Engel (2002), the greater volatility of the exchange rate and muted sensitivity of the economy in a low pass-through environment also occurs in models in which low exchange rate pass-through is modelled using sticky prices/local currency pricing rather than the pricing-to-market framework used here.

In our benchmark calibration with trade price elasticities of unity, we find that these two effects are offsetting, and, as in partial equilibrium, the extent of exchange rate pass-through to import prices is not systematically related to external adjustment. However, these general equilibrium effects need not offset each other completely. For instance, even with trade price elasticities of unity, we find that if domestic absorption moves sluggishly in response to shocks, the nominal trade balance may actually adjust more in a low pass-through environment.<sup>4</sup>

As the price elasticities of import and export demand move above one, the response of real variables—including trade volumes—is magnified, while moves in the exchange rate and the terms of trade become more muted. Accordingly, higher pass-through is associated with increased nominal adjustment in this case. Conversely, if the trade-price elasticities are less than one, a decline in import price pass-through facilitates adjustment of the nominal trade balance. We show that these conclusions are true in both partial and general equilibrium.

The remainder of our paper is organized as follows. The next section provides a brief literature review and discusses some key background issues. The following section presents our open-economy model. We then explore the features of this model, first in partial equilibrium and then in a battery of general equilibrium simulations. The final section summarizes some conclusions that emerge from our work.

## 2 Review of Empirical Literature and Some Key Issues

As background for this discussion, we provide a brief review of recent empirical evidence regarding the evolution of the exchange rate sensitivity of trade prices. Marazzi, Sheets, and Vigfusson (2005) report a sustained decline in the exchange rate sensitivity of U.S. “core” import prices (i.e., excluding computers, semiconductors, and oil), from above 0.5 in the 1970s and 1980s to roughly 0.2 during the past decade. Recent analyses by the BIS (2005) and the IMF (2005) have found broadly similar results. Campa and Goldberg (2005) do not find a decline in exchange rate pass-through to U.S. import prices, but these authors nevertheless conclude

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<sup>4</sup> The sluggish response of absorption can arise if, for example, the degree of habit persistence is relatively large, or there are costs to adjusting investment.

that pass-through to U.S. import prices is quite low. As documented by Vigfusson, Sheets, and Gagnon (2006), U.S. export prices, in contrast, continue to show little sensitivity to movements in the dollar.

There is also a growing body of work on the evolution of import price pass-through in other industrial countries. For example, Marazzi, Sheets, and Vigfusson (2005) show that pass-through to import prices has fallen significantly in recent years in Japan and has been low and stable in Germany. Research by the BIS (2005), Ihrig, Marazzi, and Rothenberg (2006), and Sekine (2006) has detected declines for the G-7 countries (albeit sometimes small declines) in the 1990-2004 period relative to previous years. The reduction in import price pass-through does not appear to be a universal phenomenon, however. For some smaller industrial countries—including, for example, Australia and Sweden—there is evidence that pass-through to import prices has remained close to one.<sup>5</sup> As far as we know, no broad studies of import price pass-through for the emerging market or developing countries have been done, presumably because of data limitations.<sup>6</sup>

We conclude this section by making two further observations. First, the price elasticities of import and export demand play a crucial role in influencing our results. As noted in the introduction, our analysis generally focuses on the case in which these elasticities are both set equal to one. This emphasis is consistent with our interpretation of the empirical evidence put forward in Hooper and Marquez (1995), Senhadji and Montenegro (1999), and Marquez (2002), who estimate these elasticities based on aggregate data and find them to be at (or sometimes even below) unity. A parallel literature, however, has focused on estimating trade price elasticities using more disaggregated data. This work has produced an array of estimates, but the reported elasticities are typically higher than those obtained using aggregate data.<sup>7</sup> For this reason, we also consider a case in which the trade price elasticities are set equal to three.

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<sup>5</sup> For Australia, see Ellis (2004) and Heath, Roberts, and Bulman (2004); for Sweden, see Nessen (2004) and Adolphson (2004).

<sup>6</sup> Working with a panel of over 70 countries, Frankel, Parsley, and Wei (2005) focus on the prices of eight narrowly defined imported goods. They find that for these goods exchange rate pass-through to unit import values at the dock averaged around 0.6 during the 1990s and actually appears to have trended up over the period.

<sup>7</sup> See McDaniel and Balistreri (2003) for a review of this literature.

Throughout this paper, we discuss two notions of external adjustment—the first we call “real adjustment,” and the second we call “nominal adjustment.” Real adjustment entails shifts in the relative quantities of imports and exports or, equivalently, in real net exports. The second concept focuses on adjustment of nominal trade flows as summarized by the nominal trade balance. While both of these concepts are useful in gauging various aspects of external performance, we place particular emphasis on the behavior of the nominal trade balance, since it is more closely related to global current account imbalances and the evolution of the (increasingly negative) U.S. net international investment position.

### 3 The Model

Our model consists of a home and a foreign economy. These two economies have isomorphic structures so in our exposition we focus on describing only the domestic economy. The domestic economy consists of households, final good producers, intermediate good producers, and a government sector. Households supply their labor to firms and consume the economy’s final good purchased from perfectly competitive final good producers. These producers demand a variety of goods from monopolistically competitive intermediate good firms located in both the domestic and foreign economy.

These monopolistic producers set prices both at home and abroad, and we consider two alternatives for the way they set their export prices. The first is “producer currency pricing” in which an exporter’s price denominated in domestic currency is equal to its domestic price. In this case, exchange rate pass-through to import prices is complete. In our alternative specification, markets are segmented, and it is optimal for an intermediate good producer to “price to market,” as we specify demand curves in which the demand elasticity is non-constant (NCES) and differs at home and abroad. In this case, an exporter’s price will depend on the price of its competitors, which gives rise to incomplete pass-through.

### 3.1 Final Goods Producers

The economy's final good ( $A_t$ ) is used for consumption, investment, and government consumption. This final good is produced by perfectly competitive firms who purchase a continuum of differentiated, domestically-produced goods,  $A_{dt}(i)$ ,  $i \in [0, 1]$  and a continuum of imported goods,  $M_t(i)$ ,  $i \in [0, 1]$ .

A representative final good producer chooses its purchases of imports and domestically-produced goods as well as  $A_t$  to maximize its profits:

$$\max P_t A_t - \int_0^1 P_{dt}(i) A_{dt}(i) di - \int_0^1 P_{mt}(i) M_t(i) di, \quad (1)$$

subject to its demand aggregator,  $D\left(\frac{A_{dt}(i)}{A_t}, \frac{M_t(i)}{A_t}\right) = 1$ , taking prices as given. The demand aggregator is given by:

$$D\left(\frac{A_{dt}(i)}{A_t}, \frac{M_t(i)}{A_t}\right) = \left[V_{dt}^{1/\rho} + V_{mt}^{1/\rho}\right]^\rho - \frac{1}{(1+\eta)\gamma} + 1, \quad (2)$$

where  $V_{dt}$  is an aggregator of domestically-produced goods given by:

$$V_{dt} = \int_0^1 \left(\frac{1}{1+\omega}\right)^\rho \frac{1}{(1+\eta)\gamma} \left[(1+\omega)(1+\eta)\frac{A_{dt}(i)}{A_t} - \eta\right]^\gamma di, \quad (3)$$

and  $V_{mt}$  is an aggregator of imported goods given by:

$$V_{mt} = \int_0^1 \left(\frac{\omega}{1+\omega}\right)^\rho \frac{1}{(1+\eta)\gamma} \left[\left(\frac{1+\omega}{\omega}\right)(1+\eta)\frac{M_t(i)}{A_t} - \eta\right]^\gamma di. \quad (4)$$

Our demand aggregator is similar to Gust, Leduc, and Vigfusson (2006), who extend the one discussed in Dotsey and King (2005) to an international environment.<sup>8</sup> It shares the central feature that the elasticity of demand is nonconstant with  $\eta \neq 0$ , and the (absolute value of the) demand elasticity can be expressed as an increasing function of a firm's relative price, when  $\eta < 0$ . This feature has proven useful in the sticky price literature, because it reduces a firm's incentive to raise its price after an expansionary monetary shock in the context of a model in which other firms have already preset their prices. Another important implication of this

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<sup>8</sup>Also, see Gust, Leduc, and Vigfusson (2006) for a discussion of the properties of this demand aggregator.

aggregator, more relevant for us, is that exchange-rate pass-through to import prices can be incomplete when the elasticity of demand is increasing in a firm's relative price.<sup>9</sup>

Profit maximization by the representative final good producer implies that its demand for import good  $i$  is given by:

$$M_t(i) = \frac{\omega}{1 + \omega} \left[ \frac{1}{1 + \eta} \left( \frac{P_{mt}(i)}{P_{mt}} \right)^{\frac{1}{\gamma-1}} \left( \frac{P_{mt}}{\Gamma_t} \right)^{\frac{\rho}{\gamma-\rho}} + \frac{\eta}{1 + \eta} \right] A_t. \quad (5)$$

In equation (5),  $P_{mt}$  is a price index consisting of all import prices:

$$P_{mt} = \left( \int_0^1 P_{mt}(i)^{\frac{\gamma}{\gamma-1}} di \right)^{\frac{\gamma-1}{\gamma}}, \quad (6)$$

and  $\Gamma_t$  is a price index consisting of the prices of a firm's competitors and is given by:

$$\Gamma_t = \left[ \frac{1}{1 + \omega} P_{dt}^{\frac{\gamma}{\gamma-\rho}} + \frac{\omega}{1 + \omega} P_{mt}^{\frac{\gamma}{\gamma-\rho}} \right]^{\frac{\gamma-\rho}{\gamma}}, \quad (7)$$

where  $P_{dt}$  is defined similar to equation (6) except that it consists of the prices of domestically-produced goods.

As in Dotsey and King (2005), when  $\eta \neq 0$ , the demand curve for good  $i$  has an additive linear term which implies that the elasticity of demand for good  $i$  depends on  $P_{mt}(i)$  relative to the price of a firm's competitors,  $\Gamma_t$ . Our aggregator differs from Dotsey and King (2005) by aggregating over foreign goods, and allowing for home bias in consumption expenditures. Accordingly, the aggregator of Dotsey and King (2005) can be viewed as a special case in which  $\rho = 1$  and  $\omega = 0$ . Another property of our aggregator is that it nests an Armington (1969) aggregator so that the elasticity of substitution between a home and foreign good can differ from the demand elasticity for two home goods.<sup>10</sup> This different elasticity occurs when  $\rho \neq 1$ ,

<sup>9</sup> See also Bergin and Feenstra (2001), who demonstrate that the interaction of their NCES demand curve with sticky prices/local currency pricing is useful in accounting for the observed volatility and persistence of the exchange rate.

<sup>10</sup> More specifically, with  $\eta = 0$ , the demand aggregator can be thought of as the combination of a Dixit-Stiglitz and Armington aggregator. To see this, note that we can rewrite our aggregator as:

$$A_t = (1 + \omega) \left[ \frac{1}{1 + \omega} A_{dt}^{\frac{\gamma}{\rho}} + \frac{\omega}{1 + \omega} M_t^{\frac{\gamma}{\rho}} \right]^{\frac{\rho}{\gamma}},$$

where  $A_{dt} = \left( \int_0^1 A_{dt}(i)^{\gamma} di \right)^{\frac{1}{\gamma}}$  and  $M_t = \left( \int_0^1 M_t(i)^{\gamma} di \right)^{\frac{1}{\gamma}}$ . Thus, the elasticity of substitution between two home goods is influenced by  $\gamma$ , and the elasticity of substitution between the home and foreign good aggregates is influenced by both  $\gamma$  and  $\rho$ .

which gives the model flexibility to match empirical estimates of economy-wide markups and those of the price elasticity of aggregate trade flows.

Profit maximization implies a similar expression for the demand of  $A_{dt}(i)$  expressed as a function of  $P_{dt}(i)$ ,  $\Gamma_t$ , and  $P_{dt}$ , the price index for domestically-produced goods. It also implies that the price of the final good paid by households is given by:

$$P_t = \frac{1}{1+\eta}\Gamma_t + \frac{\eta}{1+\eta} \left[ \frac{1}{1+\omega} \int_0^1 P_{dt}(i)di + \frac{\omega}{1+\omega} \int_0^1 P_{mt}(i)di \right]. \quad (8)$$

From this expression, it is clear that the price of the final good is equivalent to the competitive price index,  $\Gamma_t$ , when  $\eta = 0$ . In general,  $P_t$  is the sum of  $\Gamma_t$  with a linear aggregator of prices for individual goods, reflecting the influence of the linear portion of the demand curves.

### 3.2 Intermediate Goods Firms

Intermediate good producers are monopolistically competitive, and each firm in the home economy sells its good to both the home and foreign final good producers. A producer utilizes capital and labor to produce its good according to:

$$Y_t(i) = Z_t K_t(i)^\alpha L_t(i)^{1-\alpha}, \quad (9)$$

where  $Z_t$  is an aggregate shock to the level of technology. Intermediate good firms purchase capital and labor from the economy's households in perfectly competitive factor markets, and we assume that capital and labor are completely mobile within a country. Thus, all domestic firms have identical marginal cost per unit of output,  $MC_t$ .

We consider two alternatives for a firm's price setting decisions. In both cases, we allow for sticky domestic prices by following Rotemberg (1982) and assuming that firm  $i$  faces a cost of adjusting its domestic price:

$$\phi_{dt}(i) = \frac{\phi_d}{2} \left( \frac{P_{dt}(i)}{P_{dt-1}(i)} - 1 \right)^2. \quad (10)$$

In our first alternative, a firm practices producer currency pricing (PCP), and its export price denominated in foreign currency is given by:

$$P_{mt}^*(i) = \frac{P_{dt}(i)}{e_t}, \quad (11)$$

where  $e_t$  is the exchange rate expressed in units of home currency per unit of foreign currency. In the PCP case, the law of one price holds. In addition, holding domestic prices fixed, an exporter will change its price one-for-one with a given percentage change in the exchange rate so that pass-through of exchange rate changes to foreign import prices will be complete.

In our other alternative, we assume that markets are segmented, allowing a firm to price to market (PTM). In this case, a firm sets its export price to maximize profits in its foreign market:

$$\max (e_t P_{mt}^*(i) - MC_t) M_t^*(i), \quad (12)$$

taking marginal cost and its demand curve,  $M_t^*(i)$ , as given. Profit maximization implies that the monopolist chooses to set its price as a markup over marginal cost:

$$P_{mt}^*(i) = \mu_{mt}^*(i) \frac{MC_t}{e_t}. \quad (13)$$

In the above, a home exporter's markup,  $\mu_{mt}^*(i)$  is given by:

$$\mu_{mt}^*(i) = \left[ 1 - \frac{1}{|\epsilon_{mt}^*(i)|} \right]^{-1},$$

where  $|\epsilon_{mt}^*(i)|$  is (the absolute value of) the demand elasticity:

$$\epsilon_{mt}^*(i) = \frac{1}{1 - \gamma} \left[ 1 + \eta \left( \frac{P_{mt}^*(i)}{P_{mt}^*} \right)^{\frac{1}{1-\gamma}} \left( \frac{P_{mt}^*}{\Gamma_t^*} \right)^{\frac{\rho}{\rho-\gamma}} \right]^{-1}. \quad (14)$$

According to equations (13) and (14), a firm's pricing decision depends not only on its marginal cost (denominated in foreign currency) but also on  $\Gamma_t^*$ , the prices of its competitors in the foreign market. We calibrate our demand aggregator to allow for strategic complementarity in price setting.<sup>11</sup> In that case,  $|\epsilon_{mt}^*(i)|$  is an increasing function of  $\frac{P_{mt}^*}{\Gamma_t^*}$  and a firm's desired markup will be a decreasing function of this relative price. As a consequence, a domestic exporter will find it desirable to lower its markup in response to a shock that raises its costs relative to its competitors, because the exporter does not want its price to deviate too far from its

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<sup>11</sup> We follow Woodford (2003) and define pricing decisions to be *strategic complements* if an increase in the prices charged for other goods increases a firm's own optimal price.

competitors' prices. In this way, pass-through of exchange-rate changes to import prices can be incomplete even in the absence of nominal price rigidities.

In the PTM alternative, a firm chooses contingency plans for domestic prices to maximize its expected discounted stream of profits from the domestic market:

$$E_t \sum_{j=0}^{\infty} \psi_{t,t+j} \{ [P_{dt+j}(i) - MC_{t+j}] A_{dt+j}(i) [1 - \phi_{dt+j}(i)] \}, \quad (15)$$

taking marginal cost, its stochastic discount factor,  $\psi_{t,t+1}$ , and the demand schedule for its good as given.<sup>12</sup> In the PCP alternative, a firm has a similar objective function except that now it takes into account that its price influences demand both at home and abroad:

$$E_t \sum_{j=0}^{\infty} \psi_{t,t+j} \{ [P_{dt+j}(i) - MC_{t+j}] (A_{dt+j}(i) + M_{t+j}(i)) [1 - \phi_{dt+j}(i)] \}. \quad (16)$$

As noted earlier, our calibrated demand curves imply a strategic complementarity in price setting, and, as in Kimball (1995) and Dotsey and King (2005), will be associated with more nominal domestic price inertia and output persistence than sticky price models with CES demand curves. This greater nominal domestic price inertia will be true regardless of whether export prices are determined according to PCP or PTM.

### 3.3 Households

The utility function of the representative household in the home country is

$$E_t \sum_{j=0}^{\infty} \beta^j \{ \log (C_{t+j} - \varkappa C_{t+j-1}^A) - \chi_0 \frac{L_{t+j}^{1+\chi}}{1+\chi} \}, \quad (17)$$

where the discount factor  $\beta$  satisfies  $0 < \beta < 1$  and  $E_t$  is the expectation operator conditional on information available at time  $t$ . As in Smets and Wouters (2003), we allow for the possibility of external habits, where a household cares about its consumption,  $C_t$ , relative to lagged aggregate consumption,  $C_{t-1}^A$ . The period utility function also depends on labor hours,  $L_t$ .

<sup>12</sup> For convenience, we have suppressed all of the state indices. In the household problem, we define  $\xi_{t,t+1}$  to be the price in period  $t$  of a claim that pays one unit of the home currency if the specified state occurs in period  $t+1$ . The corresponding element of  $\psi_{t,t+1}$  equals  $\xi_{t,t+1}$  divided by the probability that the specified state occurs.

A household faces a flow budget constraint in period  $t$  which states that its expenditures and net accumulation of financial assets must equal its disposable income:

$$P_t C_t + P_t I_t + \int_s \xi_{t,t+1} B_{Dt+1} - B_{Dt} + \frac{e_t P_{Bt}^* B_{Ft+1}}{\phi_{bt}} - e_t B_{Ft} = W_t L_t + R_{Kt} K_t + \Omega_t - T_t - P_t \phi_{It}. \quad (18)$$

A household's disposable income consists of its labor income ( $W_t L_t$ ), income from renting capital to firms ( $R_{Kt} K_t$ ), and an aliquot share of the profits of the domestic firms ( $\Omega_t$ ). Households also pay lump-sum taxes ( $T_t$ ) and purchase the final good for investment ( $I_t$ ). A household's investment augments capital according to:

$$K_{t+1} = (1 - \delta) K_t + I_t. \quad (19)$$

As in Christiano, Eichenbaum, and Evans (2005), households also pay a cost to changing the level of gross investment from the previous period:

$$\phi_{It} = \frac{\phi_I (I_t - I_{t-1})^2}{2 I_{t-1}}. \quad (20)$$

We assume that a household can engage in frictionless trading of a complete set of contingent claims with other domestic households. We denote  $\xi_{t,t+1}$  as the price of an asset that pays one unit of domestic currency in a particular state of nature at date  $t + 1$ , while  $B_{Dt+1}$  represents the quantity of such claims purchased by a household at time  $t$ .

While asset markets are complete within a country, we assume that trade in international assets is restricted to a non-state contingent nominal bond. Accordingly, in equation (18),  $B_{Ft+1}$  represents the quantity of a non-state contingent asset purchased at time  $t$  that pays one unit of foreign currency in the subsequent period, and  $P_{Bt}^*$  is the foreign currency price of the bond. We follow Turnovsky (1985) and assume there is an intermediation cost  $\phi_{bt}$  paid by households in the home country for purchases of foreign bonds, which is necessary to ensure that the model has a unique steady state.<sup>13</sup> More specifically, the intermediation costs depend on the ratio of economy-wide holdings of net foreign assets to nominal output and are given by:

$$\phi_{bt} = \exp \left[ -\phi_b \left( \frac{e_t B_{Ft+1}^A}{P_{Yt} Y_t} \right) + \nu_{bt} \right]. \quad (21)$$

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<sup>13</sup> This intermediation cost is asymmetric, as foreign households do not face these costs. Rather, they collect profits on the monopoly rents associated with these intermediation costs. As discussed in Schmitt-Grohe and Uribe (2003), this way of closing the model delivers similar dynamics to other alternative approaches.

In the above,  $\nu_{bt}$  is a mean-zero stochastic process, which we interpret as a risk-premium shock or a shock to the uncovered interest-rate parity condition. Abstracting from this shock, if the home economy in aggregate is a net lender, then a household will earn a lower return on any holdings of foreign bonds. By contrast, if the economy is a net debtor, a household will pay a higher return on any foreign debt.

While it is difficult to give the risk premium shock a structural interpretation, we see it as the nearest equivalent in general equilibrium to the partial equilibrium case in which the exchange rate is exogenous. As such, we use the risk premium shock as an illustrative device for comparing our partial and general equilibrium results. We then characterize how the transmission of other shocks on the trade balance is affected by incomplete pass-through.

In every period  $t$ , a household maximizes the utility functional (17) with respect to consumption, investment, the end-of-period capital stock, labor, holdings of domestic contingent claims, and holdings of the international asset subject to its budget constraint (18) and the evolution of capital (19). In doing so, a household takes as given prices and aggregate quantities such as lagged aggregate consumption and the aggregate net foreign asset position.

### 3.4 The Government and Monetary Policy

Some of the final good is purchased by the government so that  $A_t$  can be interpreted as total absorption:

$$A_t = C_t + I_t + G_t. \tag{22}$$

We assume that government purchases ( $G_t$ ) follow an exogenous, stochastic process and do not directly affect the utility function of the representative household. The government's budget is balanced every period which implies that lump-sum taxes are equal to government purchases.

We assume that monetary policy follows an interest rate rule:

$$\hat{i}_t = \gamma_\pi \hat{\pi}_t + \gamma_y \hat{y}_t + \varepsilon_{mt}, \tag{23}$$

where the symbol ‘ $\hat{\cdot}$ ’ denotes the logarithmic deviation of a variable from its steady state value. Hence,  $\hat{i}_t$  denotes the (gross) quarterly nominal interest rate expressed as a log-deviation

from steady state, and  $\pi_t = \frac{P_{dt}}{P_{dt-1}}$  is the quarterly rate of inflation. The interest rate rule also includes the log deviation of output from potential output, where potential output is defined as the domestic economy's level of output in the absence of sticky domestic prices. Finally,  $\varepsilon_{mt}$  is a stochastic disturbance which can be interpreted as a monetary policy shock.

## 4 Partial Equilibrium Analysis

To gain intuition for the relationship between exchange rate pass-through and the trade balance, we first consider a simple partial-equilibrium version of our model. In this partial equilibrium framework, we consider only the PTM case and focus on a symmetric equilibrium in which all intermediate good producers choose the same price (i.e.,  $P_{mt}^*(i) = P_{mt}^* \forall i$ ). Expressing variables in real terms, the log-linearized version of a home exporter's pricing decision in the PTM case (equation 13) can be written as:

$$\hat{p}_{mt}^* = \beta_x (\hat{m}c_t - \hat{q}_t), \quad (24)$$

where  $q_t = \frac{e_t P_t^*}{P_t}$  is the real exchange rate,  $\hat{p}_{mt}^* = \hat{P}_{mt}^* - \hat{P}_t^*$  is the foreign import price relative to the price of the final good, and  $\hat{m}c_t = \hat{M}C_t - \hat{P}_t$  denotes the deviation of real marginal cost from its steady state value. In equation (24),  $\beta_x$  determines the responsiveness of a firm's relative export price to real marginal cost denominated in foreign currency.<sup>14</sup> With  $\beta_x < 1$ , a home exporter finds it optimal to adjust its price in response to the prices of its competitors and will not fully pass through changes in marginal costs because of the competitive disadvantage that it implies. Since a foreign exporter behaves in an identical manner, there is a similar relationship for the price of a good imported to the home country:

$$\hat{p}_{mt} = \beta_m (\hat{m}c_t^* + \hat{q}_t). \quad (25)$$

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<sup>14</sup> To derive equation (24), we have also used the fact that  $\hat{\Gamma}_t^* = \hat{P}_t^*$ . Also, we can show that  $\beta_x = \frac{1}{1 - \eta \mu_m \left( \frac{\rho(\gamma-1)}{\gamma-\rho} \right)}$ , where the steady state markup is given by  $\mu_m = \frac{1}{\gamma + \eta(\gamma-1)}$ . In this derivation, we have used the fact that in the non-stochastic steady state all relative prices are equal to one, as the two economies are symmetric.

It is also convenient to rewrite equation (24) defining the export price in domestic currency units (i.e.,  $\hat{p}_{xt} = \hat{q}_t + \hat{p}_{mt}^*$ ):

$$\hat{p}_{xt} = \beta_x \hat{m}c_t + (1 - \beta_x)\hat{q}_t. \quad (26)$$

While a change in the exchange rate can affect a firm's pricing behavior indirectly by affecting real marginal cost in domestic currency, we abstract from this general equilibrium effect. We, thus, compute the direct effect by holding  $\hat{m}c_t$  constant and partially differentiating the prices in equations (26) and (25) with respect to the real exchange rate:

$$\frac{\partial \hat{p}_{xt}}{\partial \hat{q}_t} = 1 - \beta_x \quad \text{and} \quad \frac{\partial \hat{p}_{mt}}{\partial \hat{q}_t} = \beta_m. \quad (27)$$

According to equation (27), a one percent depreciation of the home currency (i.e., an increase in  $q_t$ ) leads to an increase in the import price paid by a home household of  $\beta_m$  and an increase in a home firm's export price of  $1 - \beta_x$ . (The corresponding import price paid by a foreign household falls by  $\beta_x$ ). Thus, we equate  $\beta_m$  with pass-through to the import price and  $1 - \beta_x$  with pass-through of the exchange rate to the export price.

With "direct" or partial equilibrium pass-through defined in this way, we now turn to examining the implications of various values of  $\beta_x$  and  $\beta_m$  for trade adjustment. In a symmetric equilibrium, we can rewrite equation (5) to express aggregate import demand as:

$$M_t = \frac{\omega}{1 + \omega} \left[ \frac{1}{1 + \eta} \left( \frac{P_{mt}}{\Gamma_t} \right)^{\frac{\rho}{\gamma - \rho}} + \frac{\eta}{1 + \eta} \right] A_t. \quad (28)$$

Log-linearizing this equation, we have:

$$\hat{M}_t = -\alpha_m \hat{p}_{mt} + \hat{A}_t, \quad (29)$$

where  $\alpha_m = \frac{\rho}{\rho - \gamma} \frac{1}{1 + \eta} > 0$  is the elasticity of aggregate imports ( $M_t$ ) with respect to its relative price. We can also derive a similar condition for foreign import demand or home export demand:

$$\hat{X}_t = \hat{M}_t^* = -\alpha_x (\hat{p}_{xt} - \hat{q}_t) + \hat{A}_t^*, \quad (30)$$

where  $\alpha_x > 0$  is the elasticity of a aggregate home exports with respect to its relative price.

The response of real exports and imports to an exchange rate change depends crucially on the values of  $\beta_x$  and  $\beta_m$ . This importance can be seen by partially differentiating  $\hat{M}_t$  and  $\hat{X}_t$  with respect to the exchange rate, holding  $\hat{A}_t$  and  $\hat{A}_t^*$  constant:

$$\frac{\partial \hat{M}_t}{\partial \hat{q}_t} = -\alpha_m \frac{\partial \hat{p}_{mt}}{\partial \hat{q}_t} = -\alpha_m \beta_m \quad \text{and} \quad \frac{\partial \hat{X}_t}{\partial \hat{q}_t} = -\alpha_x \left( \frac{\partial \hat{p}_{xt}}{\partial \hat{q}_t} - 1 \right) = \alpha_x \beta_x. \quad (31)$$

According to (31), a one percent real depreciation of the home currency induces a larger decrease in real imports when import price pass-through is high. Similarly, the depreciation leads to a larger increase in exports when the export price is insensitive to the exchange rate (i.e.,  $\beta_x = 1$  so that import price pass-through in the foreign country is complete). Thus, adjustment of real trade volumes in response to an exchange rate change will be larger when pass-through to import prices in both countries is complete.

To examine the relationship between pass-through and the nominal trade balance, it is convenient to define the ratio of nominal exports to imports,  $\tau_t = \frac{P_{xt}X_t}{P_{mt}M_t}$ . Expressing this ratio as a log-deviation from steady state:

$$\hat{\tau}_t = \hat{p}_{xt} - \hat{p}_{mt} + \hat{X}_t - \hat{M}_t, \quad (32)$$

it is clear that nominal adjustment depends on the responses of the terms of trade,  $\frac{P_{xt}}{P_{mt}}$ , and real net exports,  $\frac{X_t}{M_t}$ . Using expressions (27) and (31), the partial effect of an exchange rate change on  $\tau_t$  is given by:

$$\frac{\partial \hat{\tau}_t}{\partial \hat{q}_t} = \left( \frac{\partial \hat{p}_{xt}}{\partial \hat{q}_t} - \frac{\partial \hat{p}_{mt}}{\partial \hat{q}_t} \right) + \frac{\partial \hat{X}_t}{\partial \hat{q}_t} - \frac{\partial \hat{M}_t}{\partial \hat{q}_t} = (1 - \beta_x - \beta_m) + \alpha_x \beta_x + \alpha_m \beta_m. \quad (33)$$

The first term in the parentheses is the effect of an exchange rate change on the terms of trade, and the other two terms are the effects of the exchange rate change on real trade volumes. If the trade-price elasticities are equal to unity (i.e.,  $\alpha_x = \alpha_m = 1$ ), then nominal adjustment is independent of the pass-through assumptions, and the nominal trade balance will increase by one percent of the value of exports in response to a one percent depreciation of the home currency. In this case, nominal adjustment is independent of pass-through, because in both the home

and foreign country nominal expenditures on imports are unchanged, as movements in domestic currency prices are offset by proportionate shifts in real imports. The home trade balance improves in response to a depreciation of the home currency, however, because the unchanged foreign expenditure on imports translates into increased home-currency export receipts.

Although in partial equilibrium the response of the trade balance is independent of the pass-through assumptions when  $\alpha_x = \alpha_m = 1$ , the forces that bring about trade balance adjustment are different in a low and high pass-through environment. In a high pass-through environment (i.e.,  $\beta_x + \beta_m > 1$ ), the nominal trade balance rises in response to a depreciation, as real net exports increase enough to offset a fall in the terms of trade. By contrast, in a low pass-through environment (i.e.,  $0 \leq \beta_x + \beta_m < 1$ ), the terms of trade increase in response to a depreciation, and both the rise in the terms of trade and higher real net exports contribute to an increase in the trade balance.

If  $\alpha_x, \alpha_m > 1$ , then higher values of  $\beta_x$  and  $\beta_m$  induce greater trade balance adjustment. With  $\alpha_m > 1$ , both real and nominal imports fall in response to a depreciation. Because this decline is greater for higher values of  $\beta_m$ , a higher value of  $\beta_m$  is associated with more trade balance adjustment. Similarly, with  $\alpha_x > 1$ , real and nominal exports rise following a depreciation, and this increase is larger for higher values of  $\beta_x$ .

It is also interesting to note that the usual Marshall-Lerner condition needs to be modified in an environment with incomplete pass-through. This condition states that for a depreciation of the domestic currency to lead to a rise in the trade balance, the sum of the export and import price elasticities must be greater than one (i.e.,  $\alpha_x + \alpha_m > 1$ ). However, this condition is derived assuming complete pass-through. From equation (33), we can see that for a depreciation to induce an improvement in the trade balance, it must be true that:

$$\alpha_x \beta_x + \alpha_m \beta_m > \beta_x + \beta_m - 1. \tag{34}$$

In the complete pass-through environment ( $\beta_x = \beta_m = 1$ ), this condition is the same as the usual Marshall-Lerner condition. More generally, this modified version of the Marshall-Lerner condition states that for a depreciation of the domestic currency to lead to an increase in the trade balance, its stimulative effects on real exports and real imports must be greater than its

effect on the terms of trade. Notably, if  $\beta_x, \beta_m \leq \frac{1}{2}$ , then equation (34) is satisfied for any positive values of the trade price elasticities.

## 5 General Equilibrium Analysis

### 5.1 Three Benchmark Scenarios

Our partial equilibrium framework assumed that the exchange rate was exogenous and held variables such as home and domestic absorption constant. We now relax these assumptions by simulating the effects of various shocks in our general equilibrium model. For each of the shocks that we study, we consider three scenarios:

- *Scenario 1*: High import price pass-through in the home country and in the foreign country. In this case, both domestic exporters and foreign exporters practice producer currency pricing.
- *Scenario 2*: Low import price pass-through in the home and foreign countries. In this instance, domestic and foreign exporters both engage in pricing to market.
- *Scenario 3*: Low import price pass-through in the home country and high import price pass-through in the foreign country. In this scenario, the home country and the foreign country are no longer symmetric. Domestic exporters engage in producer currency pricing, while foreign exporters practice pricing to market. This scenario is consistent with a world in which trade prices are set in the home country and are translated abroad by movements in the exchange rate.

While all three of these scenarios are useful conceptual benchmarks, it is helpful to make a few comments about their empirical relevance for the United States. The evidence discussed above indicates that pass-through to U.S. import prices is now relatively low, which differs significantly from the features of Scenario 1. As noted above, the results for others countries are somewhat less conclusive. The evidence suggests that import price pass-through for some major countries (e.g., Japan and Germany) is also low; but for some smaller countries (e.g., Australia and Sweden), pass-through to import prices appears to have remained high. As such, the global economy at present appears to have features of both Scenario 2 and Scenario 3.

## 5.2 Model Calibration

We solve our general equilibrium model by log-linearizing the equations around the steady state. To obtain the reduced-form solution of the model, we use the numerical algorithm of Anderson and Moore (1985), which provides an efficient implementation of the method proposed by Blanchard and Kahn (1980).

For simplicity, we choose the model parameters to be the same across the two economies. Also, we calibrate the model at a quarterly frequency by setting  $\beta = (1.03)^{-0.25}$  and  $\delta = 0.025$ . The utility function parameter  $\chi$  is set to 1.5, which implies a Frisch labor supply elasticity of  $\frac{2}{3}$ , while  $\chi_0$  is chosen so that the steady state level of hours worked is normalized to unity. We set the degree of habit persistence in consumption,  $\varkappa$ , equal to 0.8, and the cost of adjusting investment,  $\phi_I$ , equal to 4, a value in line with the estimate of Christiano, Eichenbaum, and Evans (2005). We choose a small value for the financial intermediation cost,  $\phi_b = 0.0001$ , which is necessary to ensure that net foreign assets are stationary.

The Cobb-Douglas production function parameter,  $\alpha$ , equals 0.36, which implies a steady state (quarterly) capital to output ratio of around 9. The steady state investment to output ratio is 23 percent, while government consumption is 16 percent of steady state output. We choose  $\omega$  so that the steady state import to output ratio is 12.5 percent. Given that trade is balanced in steady state, the export share in both economies is also 12.5 percent.

For the demand curves, we set  $\gamma = 1.03$ ,  $\rho = 0.885$ , and  $\eta = -7$ . These values imply a steady state markup over marginal cost of 22 percent and a price elasticity of aggregate trade flows of unity. In addition, in the case in which both home and foreign exporters price to market, they imply that exchange rate pass-through to import prices is about 40 percent. Using data for the past couple of decades, this value is in line with empirical estimates for the United States, but somewhat above estimates obtained from data over only the past ten to fifteen years.

We set the adjustment cost parameter for domestic prices,  $\phi_d$ , to be consistent with four-quarter contracts. For the monetary policy rule, we follow Taylor (1993) and set  $\gamma_\pi = 1.5$  and  $\gamma_y = \frac{0.5}{4}$ .

### 5.3 A 10 percent Depreciation of the Home Currency

We first consider a shock that raises the risk premium on home assets. The shock is assumed to be persistent with an AR(1) coefficient of 0.98, so that its effects die out slowly over time. As shown in the upper-left panel of Figure 1, the shock is scaled to deliver a 10 percent initial depreciation of the real exchange rate. (In the figure, an upward movement indicates a depreciation.) Given the differing extent of pass-through in the three scenarios, risk premium shocks of varying magnitudes are required to deliver the same initial 10 percent depreciation. This scaling of the risk premium shock allows us to isolate the additional effect on the trade balance arising from changes in home and foreign absorption relative to the partial equilibrium results. Later, we explicitly take into account the endogeneity of the exchange rate and examine how its response varies across the three scenarios.

When import price pass-through at home and abroad is high (Scenario 1), home consumer prices post comparatively large initial rises, and home output moves well above potential. This elicits a relatively aggressive monetary policy response and results in a higher real interest rate than in the other two cases. This rise in the real interest rate, in turn, causes the real exchange rate to begin to retrace its initial decline and brings the output gap back toward baseline, as the compression of domestic demand offsets a rise in net exports. In the other two scenarios, where import price pass-through in the home country is low, the effects are generally similar but smaller in magnitude.

We turn now to the behavior of the external sector. As shown in the upper-left panel of Figure 2, when home import price pass-through is high (Scenario 1), the import price relative to the consumer price level jumps up, closely tracking the exchange rate as foreign exporters maintain the price in their domestic currencies.<sup>15</sup> For the other two scenarios, moves in the relative import price are more subdued, consistent with the lower pass-through. As seen in the upper-right panel, real imports fall sharply in the high pass-through case partly in response to the rise in relative import prices, while real imports decline more moderately in the two

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<sup>15</sup> Throughout this paper we consider the behavior of trade prices relative to the price of domestic and foreign consumer goods. We do this to abstract from trends in absolute price levels (arising from monetary policy actions), which cloud the analysis and are not material to the interpretation of our results.

scenarios in which pass-through is low.

The lower-left panel shows that nominal imports fall in all three scenarios, as the declines in import quantities more than offset rises in import prices. The decline in nominal imports is largest when pass-through is high in both countries and smallest when pass-through is low in both countries. As noted above, in partial equilibrium and with unitary import-price elasticities, nominal expenditure on imports is unaffected by a move in the exchange rate. Thus, the decline in nominal imports relative to baseline in all three scenarios is driven by general-equilibrium feedback effects, as tighter monetary policy slows domestic absorption, which—in turn—weighs on real and nominal imports. These feedback effects are most pronounced when pass-through is high or, equivalently, when domestic prices and output are most sensitive to the exchange rate.

We now examine the behavior of the home country's exports. High import price pass-through in the foreign market means that exporters maintain their domestic-currency prices in the face of exchange rate changes. Accordingly, as shown in the upper-left panel of Figure 3, there is comparatively little movement in the price of exports relative to consumption goods in the two cases in which import price pass-through in the foreign market is high (Scenarios 1 and 3). In contrast, when import price pass-through in the foreign market is low (Scenario 2), the home currency price of exports moves up markedly. As shown in the upper-right panel, in the cases with high foreign import price pass-through, the export price—expressed in terms of foreign currency (or, equivalently, the foreign import price)—falls significantly; and, as seen in the lower left-panel, the quantity of home exports rises correspondingly. When pass-through in the foreign market is low, the price in terms of foreign currency falls more modestly, and the volume of home exports consequently rises only a little.

The bottom-right panel shows the behavior of the home country's nominal exports. In all three scenarios, we see a marked rise in nominal exports, but the impetus for the rise differs significantly with pass-through. In the low pass-through case, Scenario 2, quantities move relatively little, but domestic-currency prices step up with the exchange rate. In the other two cases, the export price in domestic-currency terms is little changed, but quantities rise briskly.

As noted above, in partial equilibrium, the home country's export earnings rise proportionately with the fall in the exchange rate; thus, a one percent depreciation of the exchange rate raises home export revenues by one percent. In these simulations, nominal exports move more than one-for-one with the exchange rate, indicating that additional general equilibrium effects are at work. Most important, an easing of monetary policy abroad, in response to the appreciation of the foreign currency, stimulates foreign demand and consequently raises the home country's exports. This effect is largest in Scenarios 1 and 3—when foreign import price pass-through is high and, as a result, when the monetary policy response abroad is relatively aggressive.

We now look at several measures of the home country's external balance to assess the bottom-line impact on external adjustment. First, to assess the implications for real trade volumes, we consider the evolution of the ratio of real exports to real imports, which we call the "real trade balance." As shown in the upper-left panel of Figure 4, when import price pass-through is low in both countries, adjustment in the real trade balance is relatively muted. In contrast, real adjustment is most significant when import price pass-through is high in both countries—in this case we see a significant rise in real exports and a significant drop in real imports. The case in which import price pass-through is low at home but high abroad is between the two others, reflecting a large response from real exports but a smaller response from real imports.

We take the ratio of nominal exports to nominal imports as our measure of the nominal trade balance. As displayed in the upper-right panel, the results here are much more similar across the three scenarios than is the case for the real trade balance; shifts in the terms of trade (i.e., export prices relative to import prices) tend to offset the effects of real adjustment. Specifically, as shown in the lower-left panel, when import price pass-through is high in both countries, the domestic country's terms of trade decline significantly as import prices rise relative to export prices. In the case in which pass-through is low in both countries, export prices rise a little more than import prices, and the terms of trade improve slightly. The results for the asymmetric case lie between the other two cases.

Thus, the nominal trade balance improves in all three scenarios. In the high pass-through world, adjustment occurs as large declines in real imports and increases in real exports are offset by a significant deterioration in the terms of trade. When import price pass-through at home and abroad is low, quantities move by less, but the terms of trade make a positive contribution to the improvement in the nominal trade balance. In the asymmetric case, adjustment is driven mainly by a surge in export quantities. The results for the trade balance as a share of GDP (the lower-right panel) are broadly similar to those for the ratio of nominal exports to nominal imports.

In partial equilibrium, the response of the nominal trade balance to changes in exchange rates is the same regardless of the degree of exchange rate pass-through, given our maintained assumptions. Thus, the fact that the three scenarios manifest varying degrees of improvement in the nominal trade balance reflects the differing general equilibrium effects on activity and absorption under differing pass-through assumptions.

## 5.4 An Identical Shock to the Risk Premium

Building on the results from the first simulation, our second simulation introduces another important general equilibrium effect. Specifically, the previous simulation modulated the risk-premium shock in the three scenarios to deliver an initial 10 percent depreciation of the exchange rate. In contrast, this second simulation considers a shock to the risk premium on home assets that is identical in each of the three scenarios. As shown in the upper-left panel of Figure 5, this shock causes the exchange rate to depreciate by somewhat less than 10 percent in Scenario 1 (when import price pass-through at home and abroad is high), by somewhat more than 10 percent in Scenario 2 (when import price pass-through at home and abroad is low), and by exactly 10 percent in Scenario 3 (when import price pass-through is low at home but high abroad).

These contrasting outcomes reflect the fact that the underlying structure of the home and foreign economies differs across the three scenarios. As we have shown in the previous simulation, with higher pass-through, the depreciation of the home currency puts greater upward

pressure on domestic prices and output and, accordingly, leads to larger rises in domestic interest rates. This more aggressive tightening of monetary policy when pass-through is high also serves to limit the initial depreciation of the exchange rate.<sup>16</sup> By symmetric logic, the upfront depreciation of the exchange rate is relatively large when pass-through is low.

In comparing the results of this simulation and the previous simulation, a useful observation is that by construction the exchange rate depreciates the same amount in Scenario 3 in both simulations. As such, results for this scenario are identical to their counterparts in the previous figures. With this observation in hand, it becomes clear that the pattern of responses of the real interest rate and absorption in this simulation is generally consistent with that in the previous simulation. That said, the magnitude of the responses across the scenarios is more similar in this simulation, as there are smaller moves in the high-pass through case than in the previous simulation and larger moves in the low pass-through case. This reflects that in the high pass-through scenario the initial depreciation is more muted than in the previous simulation, while in the low pass-through scenario the depreciation is larger.

As shown in the top-right panel, we continue to see greater adjustment of the real trade balance in the high pass-through case, but these results are also more similar across the three scenarios than was the case in the first simulation. Specifically, for the high pass-through case, the smaller depreciation of the exchange rate and the smaller decline in absorption translate into a smaller decline in real imports; similarly, with less support from the exchange rate—and with foreign demand also less supportive—real exports rise by less than in the previous simulation. The results for the low pass-through case are symmetric. As in the previous simulation, however, differences in the performance of the real trade balance are partially offset by moves in the terms of trade—most notably for the high pass-through case.

The bottom-right panel shows the implications for the nominal trade balance. The striking result is that the path of the trade balance across the three scenarios is quite similar, at least after the first few quarters. This suggests that the additional general equilibrium effect considered in this simulation—the fact that a given risk premium shock results in a larger move

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<sup>16</sup> By the same token, when pass-through abroad is high, interest rates there fall by more, which further limits the upfront depreciation of the domestic currency.

in the exchange rate when pass-through is low—roughly offsets the effects operating through absorption that were highlighted in the first simulation. More generally, under our benchmark calibration, we find that the adjustment of the nominal trade balance in response to a similar-sized risk premium shock does not vary systematically with pass-through. This conclusion is similar in spirit to our partial equilibrium results discussed above.

Notably, however, the results of this simulation are still quite consistent with the bottom-line implications of the first simulation: When pass-through is low, the exchange rate must depreciate more to deliver a given amount of nominal adjustment. The key insight here is that the additional exchange rate depreciation that is required arises as an endogenous response to moves in interest rates. A risk premium shock elicits less tightening of monetary policy with low pass-through and, as such, the currency depreciates more when pass-through is low.

## 5.5 Other Types of Shocks

So far, we have illustrated how the extent of exchange rate pass-through affects trade adjustment using shocks to the risk premium. Since it is difficult to give these shocks a structural interpretation, we now demonstrate that our results are applicable across a broad set of shocks. Accordingly, Table 1 displays results for a contraction in government spending, a monetary expansion, and an improvement in technology, and (for the sake of comparison) a risk premium shock. In each case, the trade price elasticities are assumed to be near unity, and the shocks are scaled such that the exchange rate depreciates 1 percent in the low pass-through scenario after eight quarters.

The results of these additional simulations broadly confirm the conclusions reported above. The following features are particularly notable. First, for reasons highlighted in the previous section, the exchange rate depreciates less in the high pass-through scenario than in the low pass-through scenario for all four types of shocks. Second, the moves in absorption in the high pass-through case are systematically less supportive of imports (i.e., the change in absorption is either less positive or more negative) than in the low pass-through case, as monetary policy consistently tightens more when pass-through is high. Third, for each shock, the change in the

real trade balance in the high pass-through case is either more positive or less negative than in the low pass-through case. This reflects the fact that absorption is less supportive of imports in the high pass-through case; in addition, although the exchange rate depreciates less in the high pass-through case, real variables (including imports and exports) are more sensitive to a given move in the exchange rate when pass-through is high. Fourth, as in the two simulations above, the terms of trade deteriorate markedly in the high pass-through case but improve, although typically only slightly, in the low pass-through case. Finally, with moves in the terms of trade offsetting differing moves in the real trade balance, we again find that the impact on the nominal trade balance is quite similar in the high pass-through and low pass-through scenarios.

## **5.6 Sensitivity Analysis**

In our previous simulations, we have shown that the nominal trade balance is less sensitive to a given move in the exchange rate when pass-through is low. However, low pass-through also means that the exchange rate tends to move more in response to a given shock. The relative importance of these offsetting effects depends on the structural features of the economy. To explore this observation further, we now consider two alternative calibrations of our model. In the first, the trade price elasticities are greater than unity. In the second, absorption moves relatively sluggishly. In each case, we compare the results to those reported in our second simulation (Section 5.4).

### **5.6.1 Higher Trade Price Elasticities**

We also consider an alternative in which the trade price elasticities are set equal to three. These values were chosen to be consistent with our reading of literature suggesting that trade price elasticities estimated using disaggregated data are typically higher than those based on macro data. The risk premium shock that we use here is identical to that in the second simulation, but—as displayed in the top-left panel of Figure 6—the exchange rate now responds much less in all three scenarios. This result reflects the fact that with the larger trade price elasticities, volumes of imports and exports and, hence, real net exports are more sensitive to moves in

the exchange rate. This induces a more sustained tightening of monetary policy than was seen in the previous simulation. (The initial moves in monetary policy are not significantly different than before, but the real interest rate stays above baseline more persistently.) The more sustained response of monetary policy also means that absorption stays below baseline somewhat more persistently.

As shown in the top-right panel, the real trade balance in all three cases rises much more significantly in this simulation than in the second simulation. This reflects that import and export demand are now more sensitive to the risk premium shock, as the effects of the higher trade price elasticities more than offset the fact that the dollar depreciates by less; in addition, the somewhat longer-lived decline in absorption weighs on real imports. In contrast, given the more muted response of the real exchange rate, shifts in trade prices and, thus, in the terms of trade are more muted than in the second simulation. As such, shifts in the terms of trade are now insufficient to offset the moves in real trade quantities, which have been magnified by the higher trade price elasticities. Consequently, the extent of pass-through now affects the degree of nominal adjustment—with the trade balance as a share of GDP (the bottom-right panel) rising significantly more in the high pass-through case than in the low pass-through case. It is also noteworthy that in each scenario, the responsiveness of the nominal trade balance is more pronounced than before, as the higher trade price elasticities and the higher resulting sensitivity of real trade volumes to the exchange rate lifts the nominal trade balance.

### 5.6.2 Greater Habit Persistence and Investment Adjustment Costs

In this section, we consider a scenario in which absorption in both the home and foreign economies responds more sluggishly to shocks than in the previous simulations. This is achieved by increasing the habit persistence parameter ( $\varkappa$ ) from 0.8 to 0.95, and the cost of adjusting investment ( $\phi_I$ ) from 4 to 15. The shock is the same as in the second simulation, and the trade price elasticities are set equal to one. With this parameterization of the model, we find that the nominal trade balance actually moves more in the low pass-through case.

The results of this simulation are reported in Figure 7. Compared with the second simula-

tion, the increased sluggishness of private spending abroad means that domestic exports—and, hence, the domestic output gap—respond relatively slowly. The upfront contraction in absorption is also less pronounced, reflecting the greater degree of habit persistence and cost of adjusting investment. As shown in the upper-right panel, the real trade balance consequently moves less in each scenario than was the case in the second simulation, with the response in the high pass-through case being particularly compressed. In contrast, the moves in the terms of trade are similar to those in Figure 5, reflecting the comparable pattern and magnitude of exchange rate changes. The net result is that the nominal trade balance improves more in the low pass-through case, as the reaction of the terms of trade now more than offsets the compressed response of the real trade balance. The intuition for this result is that in the second and third scenarios low pass-through already constrains the response of the real economy. As such, the incremental effects of more sluggish absorption are felt most strongly in the high pass-through environment.

## 6 Conclusion

In this paper, we have developed an open economy DGE model in which firms optimally choose to vary their markups, allowing pass-through to be incomplete. We have used this model to study the relationship between exchange rate pass-through and external adjustment.

One notable result that has emerged from our work is that real economic variables—including absorption and real exports and imports—tend to respond less to a given-sized shock when pass-through is low. This reflects the fact that with low pass-through foreign exporters absorb a portion of the shock into their margins. As a result, domestic inflation is less sensitive to moves in the exchange rate, and the required shift in the stance of monetary policy is correspondingly less pronounced. These features of the low pass-through world tend to limit adjustment of the nominal trade balance, holding all else equal. But the fact that monetary policy moves less when pass-through is low gives rise to another important effect, which has offsetting implications for the nominal trade balance. That is, the exchange rate tends to move

more in response to a given-sized shock.

A complementary perspective on our results is that a given quantum of improvement in the nominal trade balance requires a larger move in the real exchange rate when pass-through is low. A key insight of our work, however, is that much (or all) of the additional exchange rate depreciation that is required arises as an endogenous response to moves in interest rates. The exchange rate moves more in the low pass-through world, but—as real economic variables are less sensitive to moves in the exchange rate—the broader economic implications of these larger exchange rate moves are limited.

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Table 1: Response of Trade Prices and Quantities for Alternative Shocks<sup>a,b</sup>

	Real Exchange Rate ( $q_t$ )	Absorption ( $A_t$ )	Real Trade ( $\frac{M_t^*}{M_t}$ )	Terms of Trade ( $\frac{e_t P_{mt}^*}{P_{mt}}$ )	Nominal Trade (% of GDP)
Increase in Home Risk Premium					
1. High Pass-Through	0.68	-0.37	2.37	-0.92	0.18
2. Low Pass-Through	1.00	-0.16	1.25	0.10	0.17
Government Spending Decrease					
3. High Pass-Through	0.69	-2.60	4.79	-0.92	0.48
4. Low Pass-Through	1.00	-2.38	3.69	0.05	0.47
Monetary Expansion					
5. High Pass-Through	0.43	1.62	-0.51	-0.57	-0.14
6. Low Pass-Through	1.00	1.83	-2.71	1.54	-0.15
Technology Increase					
7. High Pass-Through	0.70	0.78	1.19	-0.93	0.03
8. Low Pass-Through	1.00	0.97	0.08	0.07	0.02

<sup>a</sup>Entries refer to the response of each variable after 8 quarters. All variables except nominal trade balance are expressed as a percent deviation from steady state. The nominal trade balance is expressed as a ratio to nominal output, and the units denote the percentage point deviation from steady state.

<sup>b</sup>Each shock is calibrated to induce a 1 percent depreciation in the real exchange rate after 8 quarters in the scenario with low pass-through in each country. The AR(1) coefficient for each shock is 0.98. To induce this real depreciation, the initial decline in the government spending share is 4.2 percentage points, the monetary shock initially leads to a 125 basis point fall in the annualized real rate, and technology rises 1.25 percent in the period of the shock.

Figure 1: Response of Home Economy to 10% Depreciation  
(Deviation from Steady State)

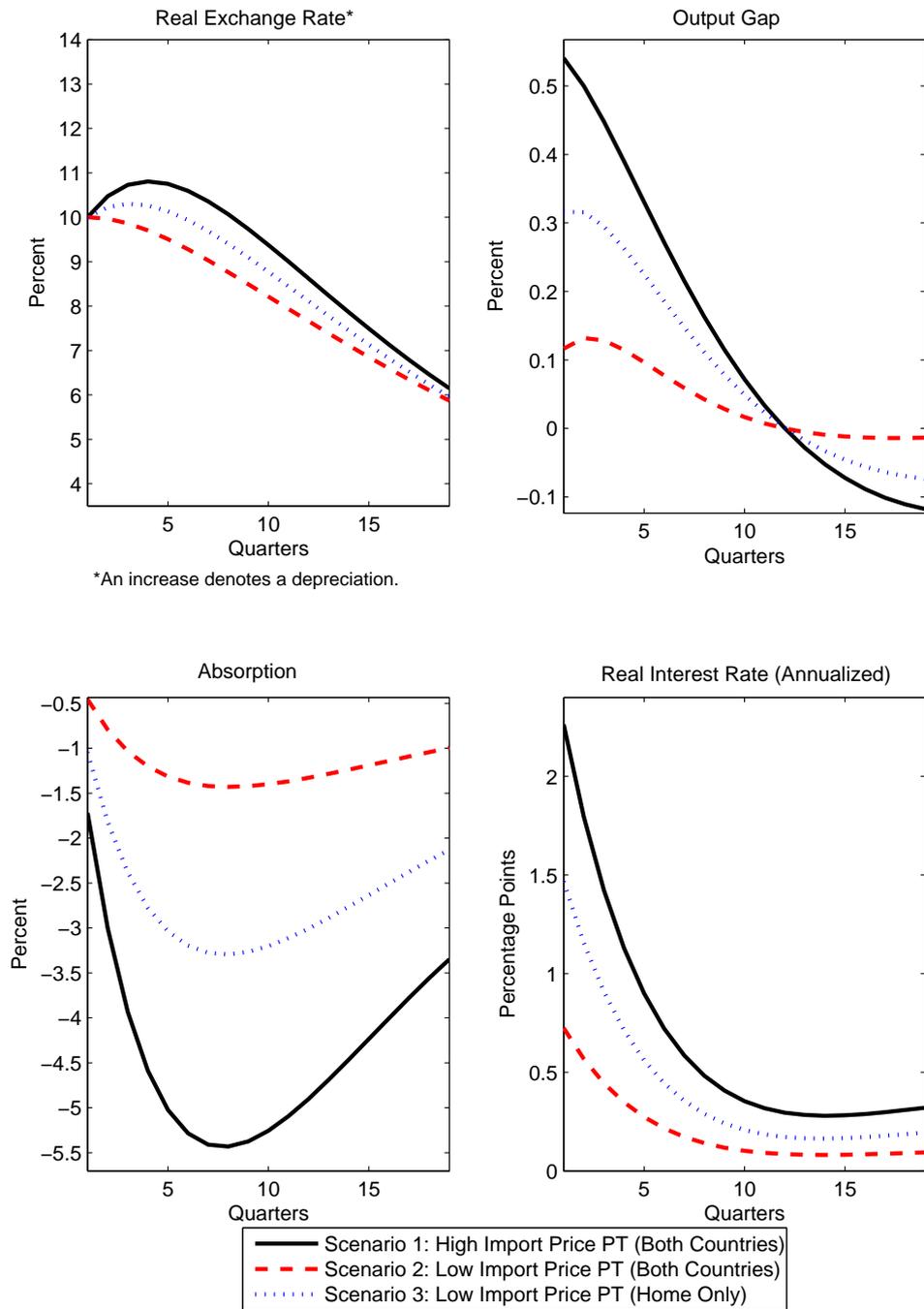


Figure 2: Response of Imports to 10% Depreciation  
(Deviation from Steady State)

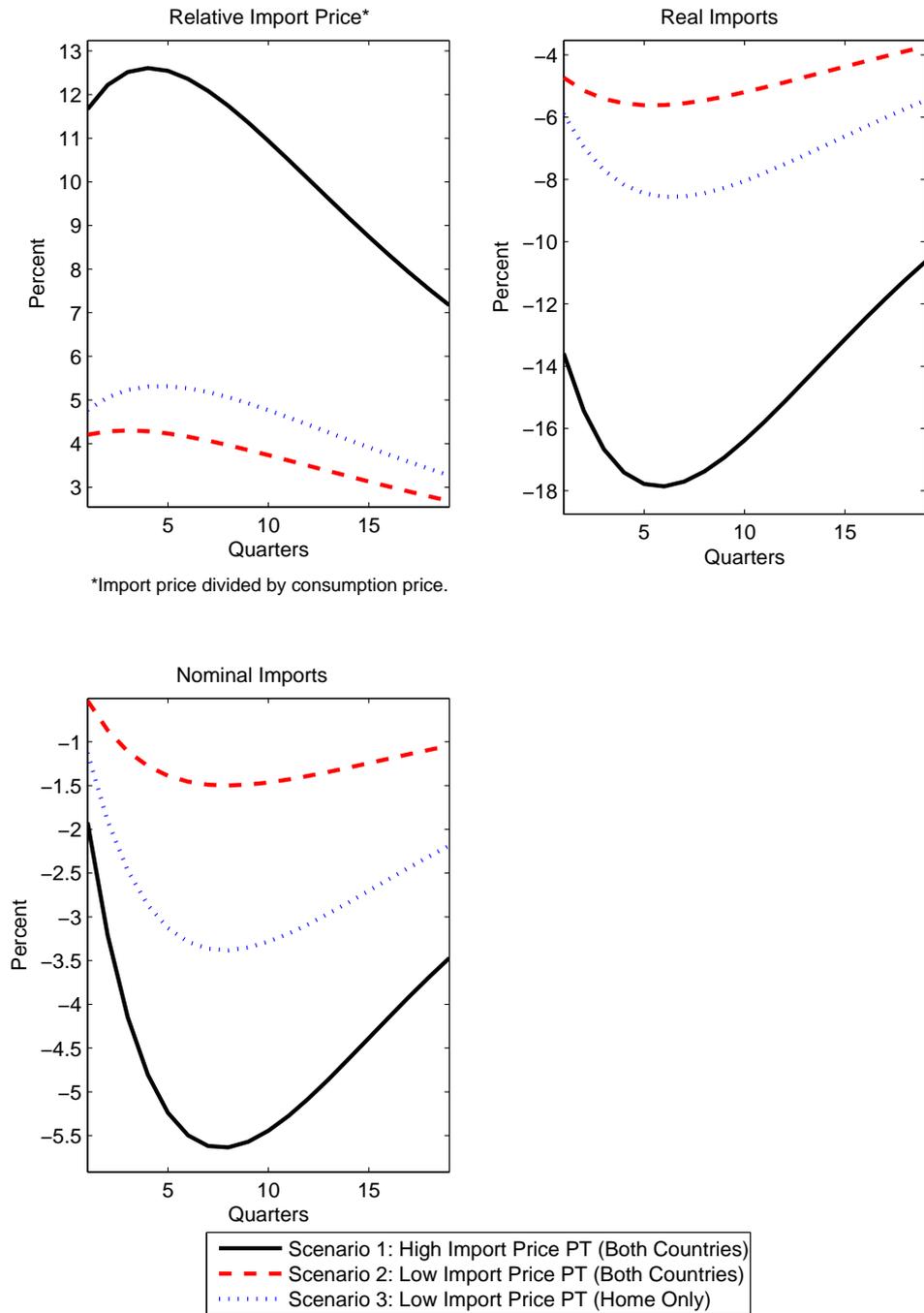


Figure 3: Response of Exports to 10% Depreciation  
(Deviation from Steady State)

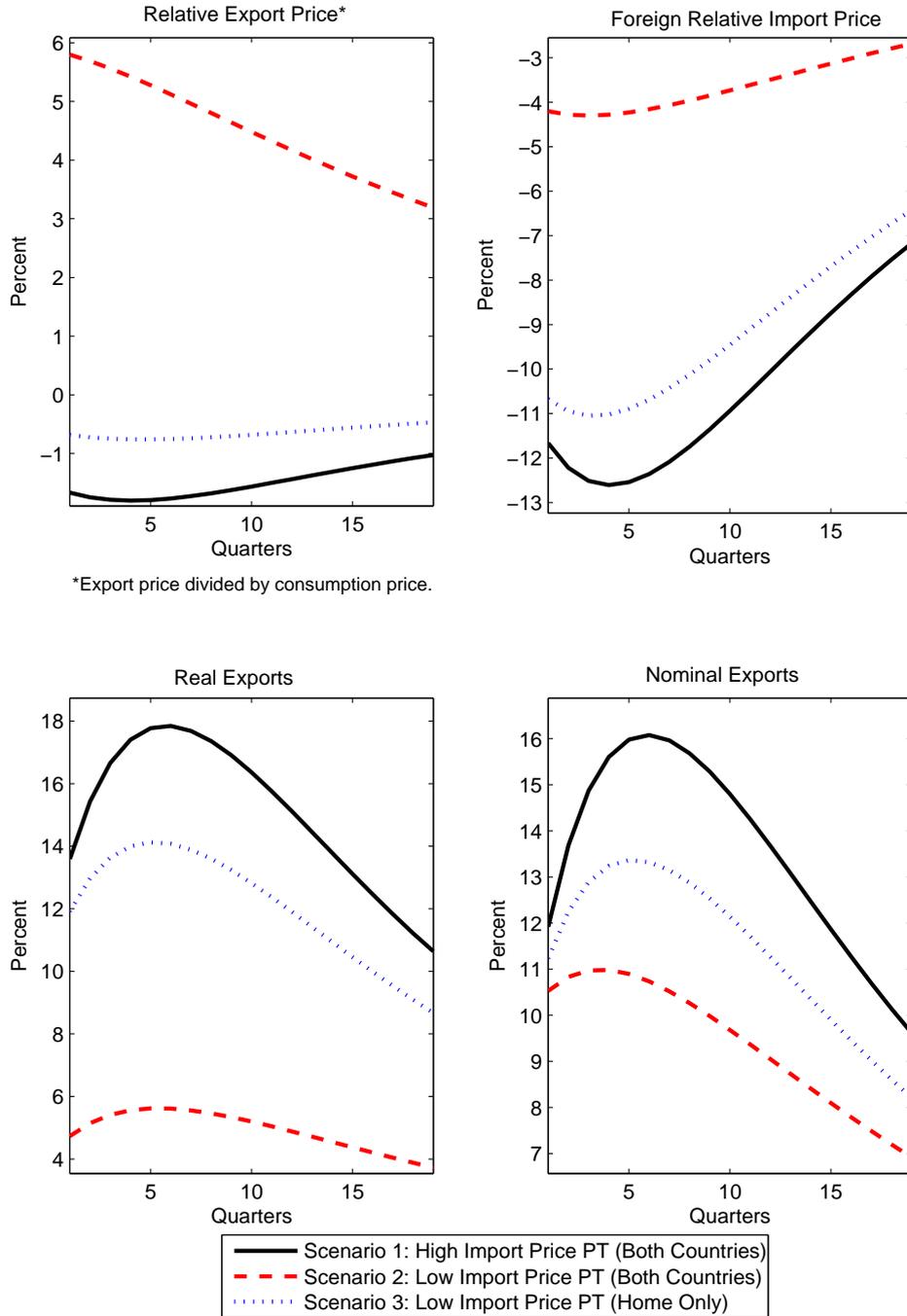


Figure 4: Response of Trade Balance to 10% Depreciation  
(Deviation from Steady State)

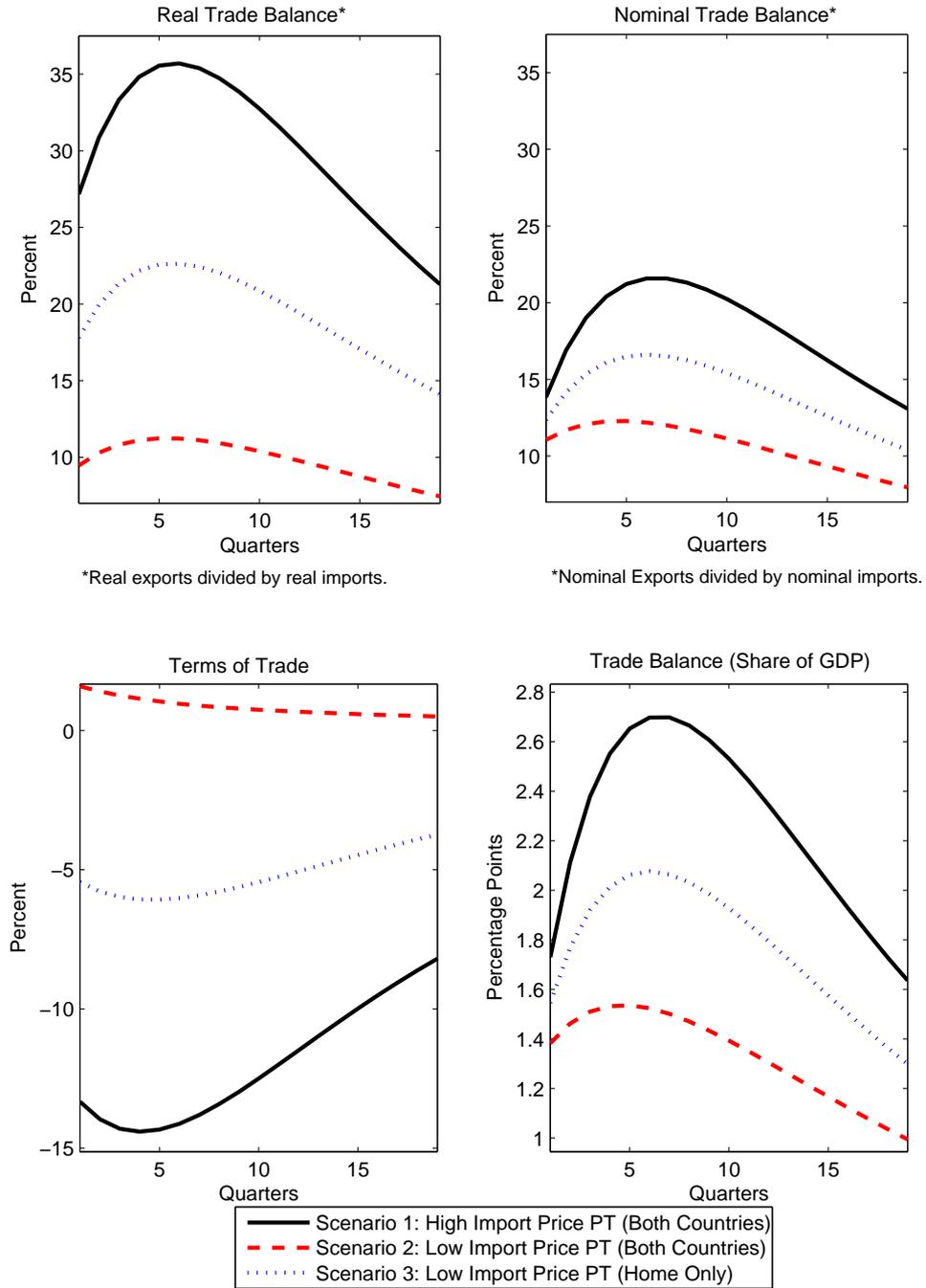


Figure 5: Response to Equally-Sized Risk Premium Shock  
(Deviation from Steady State)

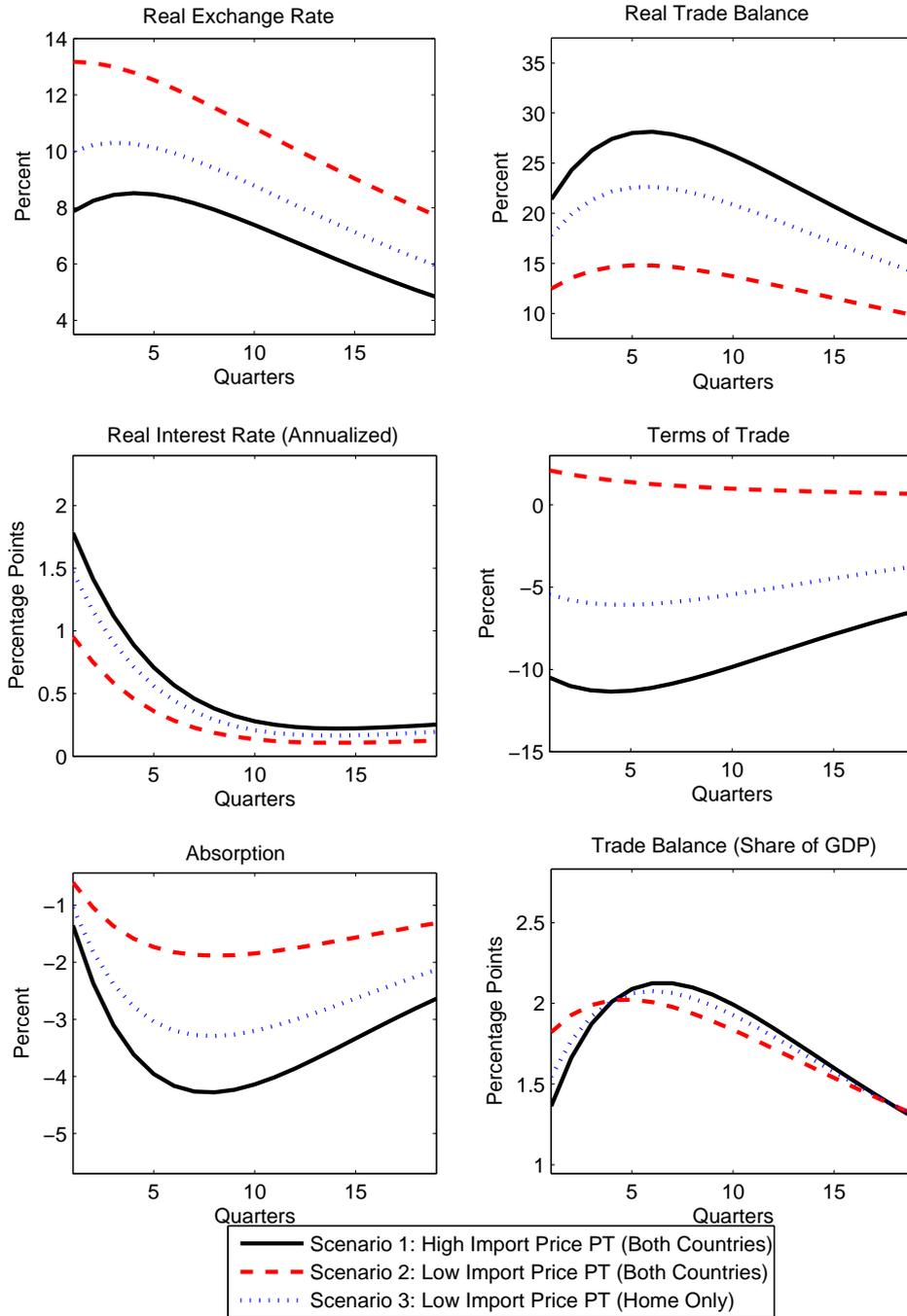


Figure 6: Response to Equally-Sized Risk Premium Shock with Higher Trade Elasticity  
(Deviation from Steady State)

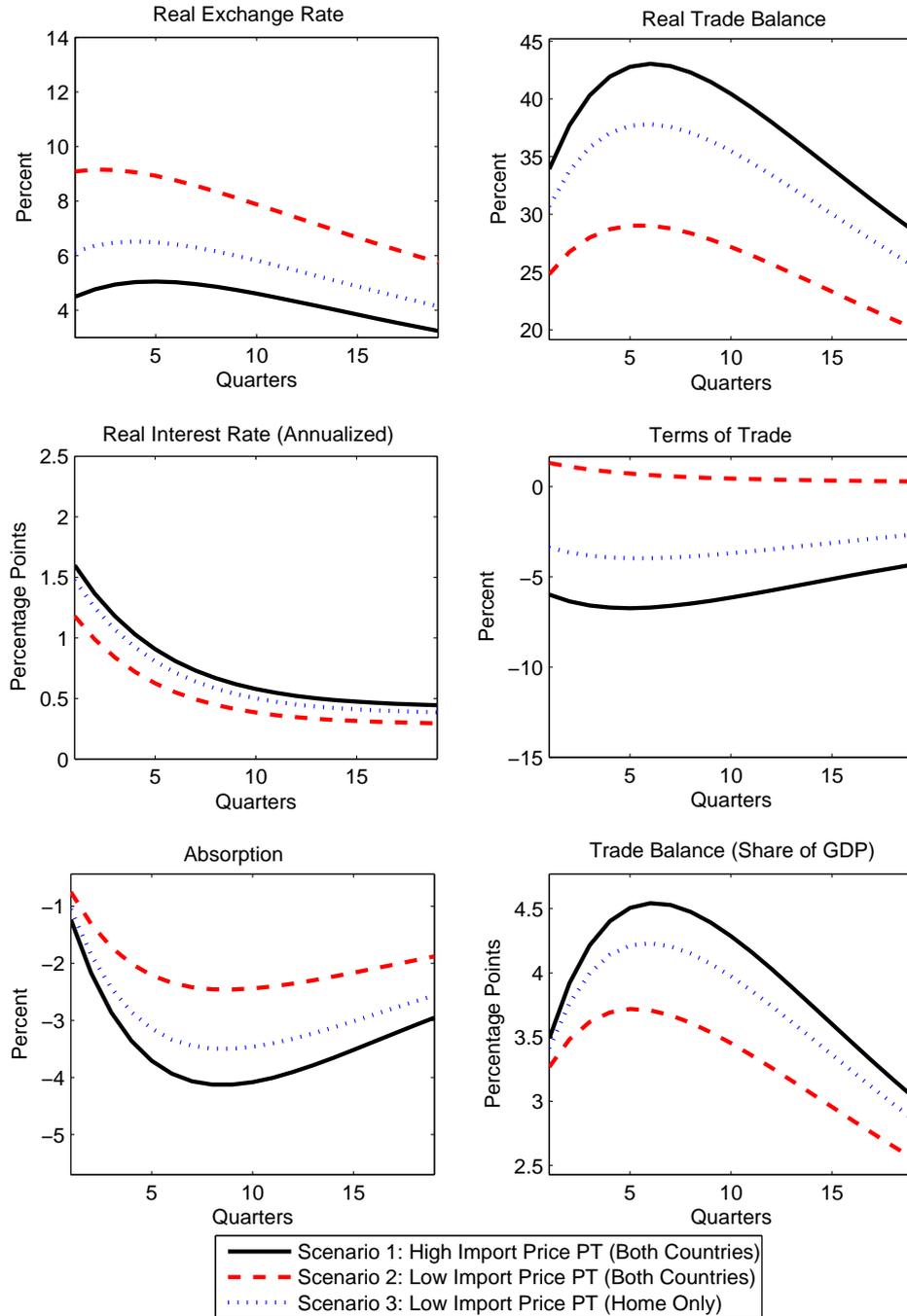


Figure 7: Response to Equally-Sized Risk Premium Shock with More Sluggish Demand  
(Deviation from Steady State)

