

Measuring the Effects of Monetary Policy: A Factor-Augmented Vector Autoregressive (FAVAR) Approach^{*}

Ben S. Bernanke, Federal Reserve Board

Jean Boivin, Columbia University and NBER

Piotr Elias, Princeton University

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Abstract

Structural vector autoregressions (VARs) are widely used to trace out the effect of monetary policy innovations on the economy. However, the sparse information sets typically used in these empirical models lead to at least two potential problems with the results. First, to the extent that central banks and the private sector have information not reflected in the VAR, the measurement of policy innovations is likely to be contaminated. A second problem is that impulse responses can be observed only for the included variables, which generally constitute only a small subset of the variables that the researcher and policymaker care about. In this paper we investigate one potential solution to this limited information problem, which combines the standard structural VAR analysis with recent developments in factor analysis for large data sets. We find that the information that our factor-augmented VAR (FAVAR) methodology exploits is indeed important to properly identify the monetary transmission mechanism. Overall, our results provide a comprehensive and coherent picture of the effect of monetary policy on the economy.

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1. Introduction

Since Bernanke and Blinder (1992) and Sims (1992), a considerable literature has developed that employs vector autoregression (VAR) methods to attempt to identify and measure the effects of monetary policy innovations on macroeconomic variables (see Christiano, Eichenbaum, and Evans, 2000, for a survey). The key insight of this approach is that identification of the effects of monetary policy shocks requires only a plausible identification of those shocks (for example, as the unforecasted innovation of the federal funds rate in Bernanke and Blinder, 1992) and does not require identification of the remainder of the macroeconomic model. These methods generally deliver empirically plausible assessments of the dynamic responses of key macroeconomic variables to monetary policy innovations, and they have been widely used both in assessing the empirical fit of structural models (see, for example, Boivin and Giannoni, 2003; Christiano, Eichenbaum, and Evans, 2001) and in policy applications.

The VAR approach to measuring the effects of monetary policy shocks appears to deliver a great deal of useful structural information, especially for such a simple method. Naturally, the approach does not lack for criticism. For example, researchers have disagreed about the appropriate strategy for identifying policy shocks (Christiano, Eichenbaum, and Evans, 2000, survey some of the alternatives; see also Bernanke and Mihov, 1998). Alternative identifications of monetary policy innovations can, of course, lead to different inferences about the shape and timing of the responses of economic variables. Another issue is that the standard VAR approach addresses only the effects of unanticipated changes in monetary policy, not the arguably more important effects of the

systematic portion of monetary policy or the choice of monetary policy rule (Sims and Zha, 1998; Cochrane, 1996; Bernanke, Gertler, and Watson, 1997).

Several criticisms of the VAR approach to monetary policy identification center around the relatively small amount of information used by low-dimensional VARs. To conserve degrees of freedom, standard VARs rarely employ more than six to eight variables.¹ This small number of variables is unlikely to span the information sets used by actual central banks, who are known to follow literally hundreds of data series, or by the financial market participants and other observers. The sparse information sets used in typical analyses lead to at least two potential sets of problems with the results. First, to the extent that central banks and the private sector have information not reflected in the VAR analysis, the measurement of policy innovations is likely to be contaminated. A standard illustration of this potential problem, which we explore in this paper, is the Sims (1992) interpretation of the so-called “price puzzle”, the conventional finding in the VAR literature that a contractionary monetary policy shock is followed by a slight increase in the price level, rather than a decrease as standard economic theory would predict. Sims’s explanation for the price puzzle is that it is the result of imperfectly controlling for information that the central bank may have about future inflation. If the Fed systematically tightens policy in anticipation of future inflation, and if these signals of future inflation are not adequately captured by the data series in the VAR, then what appears to the VAR to be a policy shock may in fact be a response of the central bank to new information about inflation. Since the policy response is likely only to partially offset the inflationary pressure, the finding that a policy tightening is followed by rising

¹ Leeper, Sims, and Zha (1996) increase the number of variables included by applying Bayesian priors, but their VAR systems still typically contain less than 20 variables.

prices is explained. Of course, if Sims' explanation of the price puzzle is correct, then all the estimated responses of economic variables to the monetary policy innovation are incorrect, not just the price response.

A second problem arising from the use of sparse information sets in VAR analyses of monetary policy is that impulse responses can be observed only for the included variables, which generally constitute only a small subset of the variables that the researcher and policymakers care about. For example, both for policy analysis and model validation purposes, we may be interested in the effects of monetary policy shocks on variables such as total factor productivity, real wages, profits, investment, and many others. Another reason to be interested in the responses of many variables is that no single time series may correspond precisely to a particular theoretical construct. The concept of "economic activity", for example, may not be perfectly represented by industrial production or real GDP. To assess the effects of a policy change on "economic activity", therefore, one might wish to observe the responses of multiple indicators including, say, employment and sales, to the policy change.² Unfortunately, as we have already noted, inclusion of additional variables in standard VARs is severely limited by degrees-of-freedom problems.

Is it possible to condition VAR analyses of monetary policy on richer information sets, without giving up the statistical advantages of restricting the analysis to a small number of series? In this paper we consider one approach to this problem, which combines the standard VAR analysis with factor analysis.³ Recent research in dynamic

² An alternative is to treat "economic activity" as an unobserved factor with multiple observable indicators. That is essentially the approach we take in this paper.

³ Lippi and Reichlin (1998) consider a related latent factor approach that also exploits the information from a large data set. Their approach differs in that they identify the common factors as the structural shocks,

factor models suggests that the information from a large number of time series can be usefully summarized by a relatively small number of estimated indexes, or factors. For example, Stock and Watson (2002) develop an approximate dynamic factor model to summarize the information in large data sets for forecasting purposes.⁴ They show that forecasts based on these factors outperform univariate autoregressions, small vector autoregressions, and leading indicator models in simulated forecasting exercises. Bernanke and Boivin (2003) show that the use of estimated factors can improve the estimation of the Fed's policy reaction function.

If a small number of estimated factors effectively summarize large amounts of information about the economy, then a natural solution to the degrees-of-freedom problem in VAR analyses is to augment standard VARs with estimated factors. In this paper we consider the estimation and properties of factor-augmented vector autoregressive models (FAVARs), then apply these models to the monetary policy issues raised above.

The rest of the paper is organized as follows. Section 2 lays out the theory and estimation of FAVARs. We consider both a two-step estimation method, in which the factors are estimated by principal components prior to the estimation of the factor-augmented VAR; and a one-step method, which makes use of Bayesian likelihood methods and Gibbs sampling to estimate the factors and the FAVAR simultaneously. Section 3 applies the FAVAR methodology and revisits the evidence on the effect of

using long-run restrictions. In our approach, the latent factors correspond instead to concepts such as economic activity. While complementary to theirs, our approach allows 1) a direct mapping with existing VAR results, 2) measurement of the marginal contribution of the latent factors and 3) a structural interpretation to some equations, such as the policy reaction function.

⁴ In this paper we follow the Stock and Watson approach to the estimation of factors (which they call "diffusion indexes"). We also employ a likelihood-based approach not used by Stock and Watson. Sargent

monetary policy on wide range of key macroeconomic indicators. In brief, we find that the information that the FAVAR methodology extracts is indeed important and leads to broadly plausible estimates for the responses of a wide variety of macroeconomic variables to monetary policy shocks. We also find that the advantages of using the computationally more burdensome Gibbs sampling procedure instead of the two-step method appear to be modest in this application. Section 4 concludes. An appendix provides more detail concerning the application of the Gibbs sampling procedure to FAVAR estimation.

2. Econometric framework and estimation

Let Y_t be an $M \times 1$ vector of observable economic variables assumed to have pervasive effects throughout the economy. For now, we do not need to specify whether our ultimate interest is in forecasting the Y_t or in uncovering structural relationships among these variables. Following the standard approach, we might proceed by estimating a VAR, a structural VAR (SVAR), or other multivariate time series model using data for the Y_t alone. However, in many applications, additional economic information, not fully captured by the Y_t , may be relevant to modeling the dynamics of these series. Let us suppose that this additional information can be summarized by an $K \times 1$ vector of unobserved factors, F_t , where K is “small”. We might think of the unobserved factors as diffuse concepts such as “economic activity” or “credit conditions”

and Sims (1977) first provided a dynamic generalization of classical factor analysis. Forni and Reichlin (1996, 1998) and Forni, Hallin, Lippi, and Reichlin (2000) develop a related approach.

that cannot easily be represented by one or two series but rather are reflected in a wide range of economic variables. Assume that the joint dynamics of (F_t, Y_t) are given by:

$$(2.1) \quad \begin{bmatrix} F_t \\ Y_t \end{bmatrix} = \Phi(L) \begin{bmatrix} F_{t-1} \\ Y_{t-1} \end{bmatrix} + v_t$$

where $\Phi(L)$ is a conformable lag polynomial of finite order d , which may contain a priori restrictions as in the structural VAR literature. The error term v_t is mean zero with covariance matrix Q .

Equation (2.1) is a VAR in (F_t, Y_t) . This system reduces to a standard VAR in Y_t if the terms of $\Phi(L)$ that relate Y_t to F_{t-1} are all zero; otherwise, we will refer to equation (2.1) as a *factor-augmented vector autoregression*, or FAVAR. There is thus a direct mapping into the existing VAR results, and (2.1) provides a way of assessing the marginal contribution of the additional information contained in F_t . Besides, if the true system is a FAVAR, note that estimation of (2.1) as a standard VAR system in Y_t —that is, with the factors omitted—will in general lead to biased estimates of the VAR coefficients and related quantities of interest, such as impulse response coefficients.

Equation (2.1) cannot be estimated directly because the factors F_t are unobservable. However, if we interpret the factors as representing forces that potentially affect many economic variables, we may hope to infer something about the factors from observations on a variety of economic time series. For concreteness, suppose that we have available a number of background, or “informational” time series, collectively

denoted by the $N \times 1$ vector X_t . The number of informational time series N is “large” (in particular, N may be greater than T , the number of time periods) and will be assumed to be much greater than the number of factors ($K + M \ll N$). We assume that the informational time series X_t are related to the unobservable factors F_t and the observable factors Y_t by:

$$(2.2) \quad X_t' = \Lambda^f F_t' + \Lambda^y Y_t' + e_t'$$

where Λ^f is an $N \times K$ matrix of factor loadings, Λ^y is $N \times M$, and the $N \times 1$ vector of error terms e_t are mean zero and will be assumed either weakly correlated or uncorrelated, depending on whether estimation is by principal components or likelihood methods (see below). Equation (2.2) captures the idea that both Y_t and F_t , which in general can be correlated, represent pervasive forces that drive the common dynamics of X_t . Conditional on the Y_t , the X_t are thus noisy measures of the underlying unobserved factors F_t . The implication of equation (2.2) that X_t depends only on the current and not lagged values of the factors is not restrictive in practice, as F_t can be interpreted as including arbitrary lags of the fundamental factors; thus, Stock and Watson (1998) refer to equation (2.2) – without observable factors – as a *dynamic factor model*.

In this paper we consider two approaches to estimating (2.1)-(2.2). The first one is a two-step principal components approach, which provides a non-parametric way of uncovering the space spanned by the common components, $C_t = (F_t', Y_t)'$, in (2.2). The

second is a single-step Bayesian likelihood approach. These approaches differ in various dimensions and it is not clear *a priori* that one should be favored over the other.

The two-step procedure is analogous to that used in the forecasting exercises of Stock and Watson. In the first step, the common components, C_t , are estimated using the first $K+M$ principal components of X_t .⁵ Notice that the estimation of the first step does not exploit the fact that Y_t is observed. However, as shown in Stock and Watson (2002), when N is large and the number of principal components used is at least as large as the true number of factors, the principal components consistently recover the space spanned by both F_t and Y_t . \hat{F}_t is obtained as the part of the space covered by \hat{C}_t that is not covered by Y_t .⁶ In the second step, the FAVAR, equation (2.1), is estimated by standard methods, with F_t replaced by \hat{F}_t . This procedure has the advantages of being computationally simple and easy to implement. As discussed by Stock and Watson, it also imposes few distributional assumptions and allows for some degree of cross-correlation in the idiosyncratic error term e_t . However, the two-step approach implies the presence of “generated regressors” in the second step. To obtain accurate confidence intervals on the impulse response functions reported below, we implement a bootstrap procedure, based on Kilian (1998), that accounts for the uncertainty in the factor estimation.⁷

⁵ A useful feature of this framework, as implemented by an EM algorithm, is that it permits one to deal systematically with data irregularities. In their application, Bernanke and Boivin (2003) estimate factors in cases in which X includes both monthly and quarterly series, series that are introduced mid-sample or are discontinued, and series with missing values.

⁶ How this is accomplished depends on the specific identifying assumption used in the second step. We describe below our procedure for the recursive assumption used in the empirical application.

⁷ Note that in theory, when N is large relative to T , the uncertainty in the uncertainty in the factor estimates can be ignored; see Bai (2002).

In principle, an alternative is to estimate (2.1) and (2.2) jointly by maximum likelihood. However, for very large dimensional models of the sort considered here, the irregular nature of the likelihood function makes MLE estimation infeasible in practice. In this paper we thus consider the joint estimation by likelihood-based Gibbs sampling techniques, developed by Geman and Geman (1984), Gelman and Rubin (1992), Carter and Kohn (1994) and surveyed in Kim and Nelson (1999). Their application to large dynamic factor models is discussed in Elias (2002). Kose, Otrok and Whiteman (2000, 2003) use similar methodology to study international business cycles. The Gibbs sampling approach provides empirical approximation of the marginal posterior densities of the factors and parameters via an iterative sampling procedure. As discussed in Appendix A, we implement a multi-move version of the Gibbs sampler in which factors are sampled conditional on the most recent draws of the model parameters, and then the parameters are sampled conditional on the most recent draws of the factors. As the statistical literature has shown, this Bayesian approach, by approximating marginal likelihoods by empirical densities, helps to circumvent the high-dimensionality problem of the model. Moreover, the Gibbs-sampling algorithm is guaranteed to trace the shape of the joint likelihood, even if the likelihood is irregular and complicated.

Identification

Before proceeding, we need to discuss identification of the model (2.1) – (2.2), specifically the restrictions necessary to identify uniquely the factors and the associated loadings. In two-step estimation by principal components, the factors are obtained entirely from the observation equation (2.2), and identification of the factors is standard.

In this case we can choose either to restrict loadings by $\Lambda^f \Lambda^f / N = I$ or restrict the factors by $F'F/T = I$. Either approach delivers the same common component $F\Lambda^f$ and the same factor space. Here we impose the factor restriction, obtaining $\hat{F} = \sqrt{T}\hat{Z}$, where the \hat{Z} are the eigenvectors corresponding to the K largest eigenvalues of XX' , sorted in descending order. This approach identifies the factors against any rotations.

In the “one-step” (joint estimation) likelihood method, implemented by Gibbs sampling, the factors are effectively identified by both the observation equation (2.2) and the transition equation (2.1). In this case, ensuring identification also requires that we identify the factors F_t against rotations of the form $F_t^* = AF_t - BY_t$, where A is $K \times K$ and nonsingular, and B is $K \times M$. We prefer not to restrict the VAR dynamics described by equation (2.1), and so we need to impose restrictions in the observation equation, (2.2). Substituting for F_t in (2.2) we obtain

$$(2.3) \quad X_t = \Lambda^f A^{-1} F_t^* + (\Lambda^y + \Lambda^f A^{-1} B) Y_t + e_t$$

Hence unique identification of the factors and their loadings requires $\Lambda^f A^{-1} = \Lambda^f$ and $\Lambda^y + \Lambda^f A^{-1} B = \Lambda^y$. Sufficient conditions are to set the upper $K \times K$ block of Λ^f to an identity matrix and the upper $K \times M$ block of Λ^y to zero. The key to identification here is to make an assumption that restricts the channels by which the Y 's contemporaneously affect the X 's. In principle, since factors are only estimated up to a rotation, the choice of the block to set equal to an identity matrix should not affect the space spanned by the estimated factors. The specific choice made restricts, however, the contemporaneous

impact of Y_t on those K variables and therefore such variables should be chosen for that block that do not respond contemporaneously to innovations in Y_t .

A separate identification issue concerns the identification of innovations in the VAR part of the model, such as identifying monetary policy innovations which is the subject of the next section. Importantly, FAVAR approach affords flexibility in identifying innovations - once factors are estimated standard procedures (e.g., structural VAR procedures as in Bernanke and Mihov, 1998) can be applied. One caveat is that use of the Gibbs sampling methodology may impose significant computational costs when complex identification schemes are employed. For example, if we impose restrictions that overidentify the transition equation, we need to perform numerical optimization at each step of the Gibbs sampling procedure. This may easily become excessively time consuming. In part for computational simplicity we use a simple recursive ordering in our empirical application below.

The two methods differ on many dimensions. A clear advantage of the two-step approach is computational simplicity. However, this approach does not exploit the structure of the transition equation in the estimation of the factors. Whether or not this is a disadvantage depends on how well specified the model is, and from a comparison of the results from the two methods we may be able to assess whether the advantages of jointly estimating the model are worth the computational costs.

3. Application: The dynamic effects of monetary policy

As discussed in the Introduction, an extensive literature has employed VARs to study the dynamic effects of innovations to monetary policy on a variety of economic variables. A variety of identification schemes have been employed, including simple recursive frameworks, “contemporaneous” restrictions (on the matrix relating structural shocks to VAR disturbances), “long-run” restrictions (on the shape of impulse responses at long horizons), and mixtures of contemporaneous and long-run restrictions.⁸

Alternative estimation procedures have been employed as well, including Bayesian approaches (Leeper, Sims, and Zha, 1996). However, the basic idea in virtually all cases is to identify “shocks” to monetary policy with the estimated innovations to a variable or linear combination of variables in the VAR. Once this identification is made, estimating dynamic responses to monetary policy innovations (as measured by impulse response functions) is straightforward.

The fact that this simple method typically gives plausible and useful results with minimal identifying assumptions accounts for its extensive application, both by academic researchers and by practitioners in central banks. Nevertheless, a number of critiques of the approach have been made (see, for example, Rudebusch, 1998). Here we focus on two issues, both related to the fact that degrees-of-freedom problems necessarily limit the number of time series that can be included in an estimated VAR. We then evaluate the

⁸ Recursive frameworks are employed, inter alia, in Bernanke and Blinder (1992), Sims (1992), Strongin (1995), and Christiano, Eichenbaum, and Evans (2000). Examples of papers with contemporaneous, non-recursive restrictions are Gordon and Leeper (1994), Leeper, Sims, and Zha (1996), and Bernanke and Mihov (1998a). Long-run restrictions are employed by Lastrapes and Selgin (1995) and Gerlach and Smets (1995). Gali (1992) and Bernanke and Mihov (1998b) use a mixture of contemporaneous and long-run restrictions. Faust and Leeper (1997) and Pagan and Robertson (1998) point out some dangers of relying too heavily on long-run restrictions for identification in VARs.

ability of FAVARs—which, potentially, can include much more information than standard VARs—to ameliorate these problems.

First, as emphasized by Bernanke and Boivin (2003), central banks routinely monitor a large number of economic variables. One rationale for this practice is that many variables may contain information that is useful in predicting output, inflation, and other variables which enter into the central bank’s objective function (Stock and Watson, 2002; Kozicki, 2001). Standard VARs of necessity include only a relatively small number of time series, implying that the information set employed by the econometrician differs from (is a subset of) that of the monetary policy-makers. To the extent that policy-makers react to variables not included in the VAR, monetary policy “shocks” and the implied dynamic responses of the economy will be mismeasured by the econometrician.⁹ A possible example of the effects of shock mismeasurement is the “price puzzle” discussed in the Introduction. We will check below whether including broader information set ameliorates the price puzzle.

Even if monetary policy shocks are properly identified, standard VAR analyses have the shortcoming that the dynamic responses of only those few variables included in the estimated VAR can be observed. As discussed in the Introduction, this limitation may be a problem for at least two reasons. First, for purposes both of policy analysis and model validation, it is often useful to know the effects of monetary policy on a lengthy

⁹ Another source of mismeasurement arises from the fact that most VAR studies typically use revised, as opposed to “real-time” data. Croushore and Evans (1999) do not find this issue to be important for the identification of monetary policy shocks, a view consistent with evidence presented in a forecasting context by Bernanke and Boivin (2003). However, Orphanides (2001) argues that assessment of Fed policy depends sensitively on whether revised or real-time data are used.

list of variables.¹⁰ Second, the choice of a specific data series to represent a general economic concept (e.g., industrial production for “economic activity”, the consumer price index for “the price level”) is often arbitrary to some degree, and estimation results may depend on idiosyncratic features of the particular variable chosen. To assess the effects of monetary policy on a concept like “economic activity”, it is of interest to observe the responses of a variety of indicators of activity, not only one or two.

The FAVAR framework is well-suited for addressing both issues. First, the estimated system (2.1)-(2.2) can be used to draw out the dynamic responses of not only the “main” variables Y_t but of any series contained in X_t . Hence the “reasonableness” of a particular identification can be checked against the behavior of many variables, not just three or four. Second, one might also consider constructing the impulse response functions of factors (or linear combinations of the factors) that can be shown to stand in for a broad concept like “economic activity.”

Empirical Implementation

We applied both the two-step and “one-step” (joint estimation) methodologies to the estimation of monetary FAVARs. In our applications, X_t consists of a balanced panel of 120 monthly macroeconomic time series (updates of series used in Stock and Watson, 1998 and 1999). These series are initially transformed to induce stationarity. The description of the series in the data set and their transformation is described in Appendix B. The data span the period from January 1959 through August 2001.

¹⁰ One approach to this problem is to assume no feedback from variables outside the basic VAR, that is, a block-recursive structure with the base VAR ordered first (see Bernanke and Gertler, 1995). However, the no-feedback assumption is dubious in many cases.

For the baseline analysis, we assume that the federal funds rate is the only observable factor, i.e. the only variable included in Y_t . In doing so, we treat the federal funds rate as a factor and interpret it as the monetary policy instrument. This is based on the presumption that monetary policy has pervasive effect on the economy, X_t . Moreover, the federal funds rate should not suffer from measurement error issues, which would otherwise imply the presence of an idiosyncratic component in the federal funds rate. The latent factors are then understood as capturing real activity and general price movements. A key advantage of this specification is that we do not have to take a stand on the appropriate measure of the real activity or inflation.

We order the federal funds rate last and treat its innovations as monetary policy “shocks”, in the standard way. This ordering imposes the identifying assumption that latent factors do not respond to monetary policy innovations within the month. To implement this identification scheme, it is useful to define two categories of variables: “slow-moving” and “fast-moving”. A “slow-moving” variable is one that is largely predetermined as of the current period, while a “fast-moving” variable – think of an asset-price – is highly sensitive to contemporaneous economic news or shocks. The classification of variables between each category is provided in the data Appendix.

As discussed above, the joint likelihood estimation only requires that the first K variables in the data set are selected from the set of “slow-moving” variables and that the recursive structure is imposed in the transition equation. For the two-step estimation this identification requires first controlling for the part of \hat{C}_t that corresponds to the federal funds rate. This is achieved in the following way. First, “slow-moving” factors, F^s_t , are

estimated as the principal components of the “slow-moving” variables. Second, the following regression,

$$(3.1) \quad \hat{C}_t = b_{F^s} \hat{F}_t^s + b_Y Y_t + e_t,$$

is estimated and \hat{F}_t constructed from $\hat{C}_t - \hat{b}_Y Y_t$. Note that in so far as \hat{F}_t^s and Y_t are correlated, so are \hat{F}_t and Y_t . Finally, the VAR in \hat{F}_t and Y_t , is estimated and identified recursively using this ordering.

The recursive assumption may be subject to criticism if components of the estimated factors, not accounted for by the federal funds rate, nevertheless respond contemporaneously to interest rate shocks. One way to address this potential problem would be to extract “slow-moving” and “fast-moving” factors from the respective blocks of data and order the “fast-moving” factors after the federal funds rate in the VAR ordering. However the “fast-moving” factors obtained in this way follow interest rate movements very closely and consequently introduce collinearity in the system. We interpret the results of this exercise as suggesting that there is little informational content in the “fast-moving” factors that is not already accounted for by the federal funds rate. We therefore adhere to our original formulation.

Empirical Results

Our main results are shown in Figures 1-4 below. Each Figure shows impulse responses with 90% confidence intervals of a selection of key macroeconomic variables to a monetary policy shock. Figures 1 and 2 show the results for the FAVAR model with 3 latent factors, estimated by principal components and likelihood methods, respectively.

We used 13 lags but employing 7 lags led to very similar results as found with the greater number of lags. Likelihood-based estimates employed 10,000 iterations of the Gibbs sampling procedure (of which the first 2,000 were discarded to minimize the effects of initial conditions). To assure convergence of the algorithm, we imposed proper but diffuse priors on parameters of the observation and the VAR equations.¹¹ Prior specifications are discussed in the Appendix. There seemed to be no problems achieving convergence, and alternative starting values or the use of 20,000 iterations gave essentially the same results. We standardize the monetary shock to correspond to a 25-basis-point innovation in the federal funds rate.¹²

An important practical question is how many factors are needed to capture the information necessary to properly model the effect of monetary policy. Bai and Ng (2002) provide a criterion to determine the number of factors present in the data set, X_t . However, this does not address the question of how many factors should be included in the VAR and due to computational constraint cannot be readily implemented in the likelihood-based estimation. To explore the effect of increasing the number of factors, we thus consider an alternative specification with 5 latent factors. The results are reported in Figures 3 and 4. Increasing the number of factors beyond this did not change qualitative nature of our results.

As we have discussed, an advantage of the FAVAR approach is that impulse response functions can be constructed for any variable in the informational data set, that is, for any element of X_t . This gives both more information and provides a more

¹¹ We have also experimented with flat priors which yielded the same qualitative results.

¹² Note that the figures report impulse responses, in standard deviation units, to 25 basis points shock in the federal funds rate.

comprehensive check on the empirical plausibility of the specification. In that respect, the most successful specification, in terms of plausibility, appears to be the two-step principal component approach with 5 factors, reported in Figure 3. In this case, the responses are generally of the expected sign and magnitude: following a contractionary monetary policy shock, real activity measures decline, prices eventually go down and money aggregates decline. The dividend yields initially jump above the steady state and eventually go down. Overall these results seem to provide a consistent and sensible measure of the effect of monetary policy. Note that we display only 20 responses of all 120 that in principle could be investigated.

The FAVAR model appears successful in capturing relevant information. First, the price puzzle is not present in our FAVAR model estimated by two-step approach, even when only three factors are included. Given that our recursive identification of the policy shocks is consistent with existing structural VARs that display the price puzzle, our result might suggest that a few factors are sufficient to properly capture the information that Sims argued might be missing from these VARs. Second, increasing the number of factors generally tends to produce results more consistent with conventional wisdom. This is particularly obvious when comparing the response of money aggregates for the 2-step approach in Figure 1 and 3: the apparent liquidity puzzle in Figures 1 disappears when more factors are included. The amount of information included in the empirical analysis is thus crucial to yield a plausible picture of the effects of monetary policy, and the FAVAR approach shows some success at exploiting this information.

But, as is obvious from the likelihood-based results reported in Figures 2 and 4, information is not all the story. In this case, responses of prices and money aggregates are

very imprecisely estimated and display both a price and liquidity puzzle. Increasing the number of factors does not appear to improve the results. This might suggest in fact that the policy shock has not been properly identified. This is a possibility that would be worth considering in future research. It is important to stress, however, that although we considered a recursive identification of the policy shock, there is nothing in our proposed approach – other than the computational constraints mentioned above – that prevents using alternative, non-recursive, identification schemes. However, the fact that the two-step approach is relatively successful with the same identification scheme might suggest that the likelihood-based estimation suffers from the additional structure it imposes, which might not be entirely supported empirically.

To assess if differences between results of the two estimation methods are due to their alternative identification or the estimation method itself, we also generated factors under the same identification. It was accomplished by setting loadings on Y to zero in the observation equation for the likelihood-based estimation and by omitting a “cleaning” regression (3.1) in case of the principal components method. These are the alternative ways of partialling out the effects of the federal funds rate from the estimated factors. As it turns out, the two sets of factors generated in this way are significantly different. The factors estimated by principal component fully explain the variance of likelihood-estimated factors but the opposite is not true. Moreover, the principal component factors have greater short run variation. We interpret these findings as evidence that the differences in identification are not the sole source of the differences in results. Since it is the likelihood method that imposes additional structure on the model, we may expect PC factors to carry more information.

While the two methods yield somewhat different responses for money aggregates and the consumer price index, overall the point estimates of the responses are quite similar. We find it remarkable that the two rather different methods, producing distinct factor estimates as discussed above, give qualitatively similar results. On the other hand, the degree of uncertainty about the estimates implied by the two methods is quite different. In fact, for some series such as the consumer price index and industrial production, the likelihood based approach yields much wider confidence intervals. This might suggest that the likelihood-based factors do not successfully capture information about these variables. The next subsection investigates this possibility by including in the set of observable factors, Y_t , the consumer price index and industrial production.

VAR – FAVAR Comparison

The benchmark specification considered thus far has the advantage of imposing minimal assumptions about the common components. In particular, we did not impose specific observable concepts for real activity or prices.

Our methodology does not prevent, however, assuming that factors, other than the federal funds rate, are also observed. For instance, we can expand Y_t to also include industrial production, as a measure of real activity and the consumer price index as a measure of prices. The resulting FAVAR system thus nests a standard VAR in the variables that are directly suggested by standard monetary models: a monetary policy indicator, a real-activity measure and a price index. By comparing the results with and without the factors, it is then possible to determine the marginal contributions of the information contained in the factors.

The impulse response functions from this alternative FAVAR specification are presented in Figure 5, for no factor, one factor and three factors. The Figure also reproduces the response obtained from the benchmark specification, with the federal funds rate assumed to be the only observable factor. The top panel shows the results from the two-step estimation and the bottom panel from the likelihood-based estimation.

When there is no factor, i.e. the standard VAR specification, there is a strong price puzzle and the response of industrial production is very persistent, inconsistent with long-run money neutrality. For the two-step estimation, adding one factor to standard VAR changes the responses dramatically. The price puzzle is considerably reduced and the response of industrial production eventually returns toward zero. In this case, adding one factor appears to be all that is needed. For the likelihood-based estimation, adding three factors tends to produce qualitatively the same responses as for the two-step estimation, although somewhat more pronounced. The estimated factors from both methods thus seem to contain useful information, beyond that already contained in the standard VAR.

An interesting aspect of these results is that the responses from the two-step estimation of the benchmark FAVAR are essentially the same as the one obtained from expanding the standard VAR by three factors from either estimation methods. This suggests that the two-step estimation of the benchmark FAVAR properly captures information about real-activity and prices, even though no such measure is imposed as observable factor. This is not the case for the likelihood-based factors and this seems to explain, at least in part, the appeared less successful for the benchmark FAVAR.

This comparison suggests that the FAVAR approach is successful at extracting pertinent information from a large data set of macroeconomic indicators. That does not mean, however, that the FAVAR approach is the only way to obtain reasonable results. There exist, of course, other VAR specifications that could lead to reasonable results over some periods. For example, some authors have “improved” their results by adding variables such as an index of commodity prices to the VAR.¹³ But unless these variables are part of the theoretical model the researcher has in mind, it is not clear on what grounds they are selected, other than the fact that they ‘work’. The advantage of our approach is to put discipline on the process, by explicitly recognizing in the econometric model the scope for additional information. As a result, the fact that adding the commodity price index – or any other variables – fixes or not the price puzzle is not directly relevant to this comparison.

Variance Decomposition

Other than impulse response functions, another exercise typically performed in the standard VAR context is variance decomposition. This consists of determining the fraction of the forecasting error of a variable, at a given horizon, that is attributable to a particular shock. Variance decomposition results follow immediately from the coefficients of the MA representation of the VAR system and the variance of the structural shocks. For instance the fraction variance of $(Y_{t+k} - \hat{Y}_{t+k})$ due to the monetary policy shock could be expressed as:

¹³ For instance, Sims (1992), Bernanke and Mihov (1998) and Christiano, Eichenbaum and Evans (1999).

$$\frac{\text{var}(Y_{t+k} - \hat{Y}_{t+k|t} | \varepsilon_t^{MP})}{\text{var}(Y_{t+k} - \hat{Y}_{t+k|t})}$$

A standard result of the VAR literature is that the monetary policy shock explains a relatively small fraction of the forecast error of real activity measures or inflation.

But, as emphasized by equation (2.2), part of the variance of the macroeconomic variables comes from their idiosyncratic component, which might reflect in part measurement error and upon which business cycle determinants should have no influence. As a result, it is not clear that the standard VAR variance decomposition provides an accurate measure of the relative importance of the structural shocks. In this context, the FAVAR framework suggests a potentially more appealing version of this decomposition, where the relative importance of a structural shock is assessed relative only to the portion of the variable explained by the common factors. More precisely, this variance decomposition for X_{it} can be expressed as:

$$\frac{\Lambda_i \text{var}(C_{t+k} - \hat{C}_{t+k|t} | \varepsilon_t^{MP}) \Lambda_i'}{\Lambda_i \text{var}(C_{t+k} - \hat{C}_{t+k|t}) \Lambda_i'}$$

where Λ_i denotes the i^{th} line of $\Lambda = [\Lambda^f, \Lambda^y]$ and $\text{var}(C_{t+k} - \hat{C}_{t+k|t} | \varepsilon_t^{MP}) / \text{var}(C_{t+k} - \hat{C}_{t+k|t})$ is the standard VAR variance decomposition based on (2.1).

Table 1 reports the results for the same twenty macroeconomic indicators analyzed in the previous Figures. These are based on the two-step estimation of the benchmark specification. The first column reports the contribution of the monetary policy shock to the variance of the forecast of the common component, at the sixty-month horizon. The second column contains the R^2 of the common component for each of these

variables.¹⁴ The product of the two columns is the equivalent of the standard VAR variance decomposition.

Apart from the interest rates and the exchange rate, the contribution of the policy shock is between 3.2% and 13.2%. This suggests a relatively small but still non-trivial effect of the monetary policy shock. In particular, the policy shock explains 13.2%, 12.9% and 12.6% of capacity utilization, new orders and unemployment respectively, and 7.6% of industrial production. Looking at the R^2 of the common component, three observations stand out. First, the factors explain a sizeable fraction of these variables, in particular for the most often used macroeconomic indicators: industrial production (70.7%), employment (72.3%), unemployment (81.6%) and the consumer price index (86.9%). This confirms that the FAVAR framework, estimated by the two-step principal component approach, does capture important dimensions of the business cycle movements. Second, given the R^2 of the common components, the discrepancies between the standard VAR decomposition and the one introduced here are considerable: for instance, the standard VAR decomposition of industrial production would imply a contribution of the policy shock equal to 5.3% instead of 7.6%, and for new orders, 8.0% instead of 12.9%. Finally, the R^2 of the common components is particularly low for the money aggregates, being 10.3% for the monetary base and 5.2% for M2. This implies that we should have less confidence on the impulse response estimates for these variables. Interestingly, these are variables for which the impulse response functions from the two estimation methods differ the most.

¹⁴ Note that since FFR is assumed to be an observed factor, the corresponding R^2 is one by construction.

4. Conclusion

This paper has introduced a method for incorporating a broad range of conditioning information, summarized by a small number of factors, in otherwise standard VAR analyses. We have shown how to identify and estimate a factor-augmented vector autoregression, or FAVAR, by both a two-step method based on estimation of principal components and a more computationally demanding, Bayesian method based on Gibbs sampling. Another key advantage of the FAVAR approach is that it permits us to obtain the responses of a large set of variables to monetary policy innovations, which provides both a more comprehensive picture of the effects of policy innovations as well as a more complete check of the empirical plausibility of the underlying specification.

In our monetary application of FAVAR methods, we find that overall the two methods produce qualitatively similar results, although the two-step approach tends to produce more plausible responses, without having to impose explicit measures of real-activity or prices. Moreover, the results provide some support for the view that the “price puzzle” results from the exclusion of conditioning information. The conditioning information also leads to reasonable responses of money aggregates. These results thus suggest that there is a scope to exploit more information in empirical macroeconomic modeling.

Future work should investigate more fully the properties of FAVARs, alternative estimation methods and alternative identification schemes. In particular, further comparison of the estimation methods based on principal components and on Gibbs sampling is likely to be worthwhile. Another interesting direction is to try to interpret the

estimated factors more explicitly. For example, according to the original Sims (1992) hypothesis, if the addition of factors mitigates the price puzzle, then the factors should contain information about future inflation not otherwise captured in the VAR. The marginal contribution of the estimated factors for forecasting inflation can be checked directly.¹⁵

¹⁵ Stock and Watson (1999) and Bernanke and Boivin (2003) have shown that, generally, factor methods are useful for forecasting inflation.

Appendix A: Estimation by Likelihood-Based Gibbs Sampling

This appendix discusses the estimation of FAVARs by likelihood-based Gibbs sampling. For further details see Elias (2002).

To estimate equations (2.1) and (2.2) jointly via likelihood methods, we transform the model into the following state-space form:

$$(A.1) \quad \begin{bmatrix} X_t \\ Y_t \end{bmatrix} = \begin{bmatrix} \Lambda^f & \Lambda^y \\ 0 & I \end{bmatrix} \begin{bmatrix} F_t \\ Y_t \end{bmatrix} + \begin{bmatrix} e_t \\ 0 \end{bmatrix}$$

$$(A.2) \quad \begin{bmatrix} F_t \\ Y_t \end{bmatrix} = \Phi(L) \begin{bmatrix} F_{t-1} \\ Y_{t-1} \end{bmatrix} + v_t$$

where Y_t is an $M \times 1$ vector of observable economic variables in whose dynamic properties we are interested, F_t is an $K \times 1$ vector of unobserved factors, and X_t is an $N \times 1$ vector of time series that incorporate information about the unobserved factors, all as described in the text. Time is indexed $t = 1, 2, \dots, T$. The coefficient matrices Λ^f and Λ^y are $N \times K$ and $N \times M$, respectively, and $\Phi(L)$ is a conformable lag polynomial of finite order d . The loadings Λ^f and Λ^y are restricted as discussed in the text. The error vectors e_t and v_t are $N \times 1$ and $(K + M) \times 1$, respectively, and are assumed to be distributed according to $e_t \sim N(0, R)$ and $v_t \sim N(0, Q)$, with e_t and v_t independent and R diagonal.

(A.1) is the measurement or observation equation, and (A.2), which is identical to (2.1), is the transition equation. Inclusion of Y_t in the measurement equation (A.1) as

well as in the transition equation (A.2) does not change the model but allows for both notational and computational simplification.

We take a Bayesian perspective, treating the model's parameters $\theta = (\Lambda^f, \Lambda^y, R, \text{vec}(\Phi), Q)$ as random variables; and where we define $\text{vec}(\Phi)$ as a column vector of the elements of the stacked matrix Φ of the parameters of the lag operator $\Phi(L)$. Likelihood estimation by multi-move Gibbs sampling (Carter and Kohn, 1994), proceeds by alternately sampling the parameters θ and the unobserved factors F_t . To be more specific, define $\mathbf{X}_t' = (X_t', Y_t')'$, $\mathbf{e}_t' = (e_t', 0)'$, and $\mathbf{F}_t' = (F_t', Y_t')'$ and rewrite the measurement and transition equations (A.1) and (A.2) as

$$(A.3) \quad \mathbf{X}_t = \Lambda \mathbf{F}_t + \mathbf{e}_t$$

$$(A.4) \quad \mathbf{F}_t = \Phi(L)\mathbf{F}_{t-1} + \mathbf{v}_t$$

where Λ is the loading matrix from (A.1) and $\mathbf{R} = \text{cov}(\mathbf{e}_t \mathbf{e}_t')$ is the covariance matrix R augmented by zeros in the obvious way. For this exposition we assume that the order d of $\Phi(L)$ equals one, otherwise we would rewrite (A.4) in a standard way to express it as a first-order Markov process (see Elias, 2002). Further, let $\tilde{\mathbf{X}}_T = (\mathbf{X}_1, \mathbf{X}_2, \dots, \mathbf{X}_T)$ be the history of \mathbf{X} from period 1 through period T , and likewise define $\tilde{\mathbf{F}}_T = (\mathbf{F}_1, \mathbf{F}_2, \dots, \mathbf{F}_T)$.

Our problem is to characterize the marginal posterior densities of $\tilde{\mathbf{F}}_T$ and θ , respectively $p(\tilde{\mathbf{F}}_T) = \int p(\tilde{\mathbf{F}}_T, \theta) d\theta$ and $p(\theta) = \int p(\tilde{\mathbf{F}}_T, \theta) d\tilde{\mathbf{F}}_T$, where $p(\tilde{\mathbf{F}}_T, \theta)$ is the joint posterior density and the integrals are taken with respect to the supports of θ and

$\tilde{\mathbf{F}}_T$, respectively. Given these marginal posterior densities, estimates of $\tilde{\mathbf{F}}_T$ and θ can be obtained as the medians or means of these densities.

To obtain empirical approximations to these densities, we follow Kim and Nelson (1999, chapter 8) and apply multi-move Gibbs sampling to the state-space model (A.3)-(A.4). The Gibbs sampling methodology proceeds as follows: First, choose a set of starting values for the parameters θ , say θ^0 . Second, conditional on θ^0 and the data $\tilde{\mathbf{X}}_T$, draw a set of values for $\tilde{\mathbf{F}}_T$, say $\tilde{\mathbf{F}}_T^1$ from the conditional density $p(\tilde{\mathbf{F}}_T | \tilde{\mathbf{X}}_T, \theta^0)$. Third, conditional on the sampled values of $\tilde{\mathbf{F}}_T$ and the data, draw a set of values of the parameters θ , say θ^1 , from the conditional distribution $p(\theta | \tilde{\mathbf{X}}_T, \tilde{\mathbf{F}}_T^1)$. The final two steps constitute one iteration, and are repeated until the empirical distributions of $\tilde{\mathbf{F}}_T^s$ and θ^s converge, where s indexes the iteration. It has been shown (Geman and Geman, 1994), that as the number of iterations $s \rightarrow \infty$, the marginal and joint distributions of the sampled values of $\tilde{\mathbf{F}}_T^s$ and θ^s converge to the true corresponding distributions at an exponential rate. In practice, though, convergence can be slow and should be carefully checked, for example by using alternative starting values. More details on each step are given below.

1. Choice of θ^0

In general, it is good practice to try a variety of starting parameter values to see if they generate similar empirical distributions. As Gelman and Rubin (1992) argue, a single sequence from the Gibbs sampler, even if it has apparently converged, may give a

“false sense of security”. At the same time, in a problem as large as the one at hand, for which computational capacity constrains the number of feasible runs, a meaningful choice of θ^0 may be advisable. An obvious choice was to use parameter estimates obtained from principal components estimation of (A.1) and the vector autoregression (A.2). We constrained these parameter estimates to satisfy the normalization, discussed in the text, that the upper $K \times (K + M)$ block of loadings Λ is restricted to be $[\mathbf{I}_K, \mathbf{0}_{K \times M}]$. We used these parameter estimates as starting values for θ in most runs, but we have confirmed the robustness of the key results for alternative starting values. For example, we also tried starting values such that (1) $\text{vec}(\Phi) = \mathbf{0}$, (2) $Q = \mathbf{I}$, (3) $\Lambda^f = \mathbf{0}$, (4) $\Lambda^y = \text{OLS estimates from the regression of } X \text{ on } Y$, and (5) $R = \text{residual covariance matrix from the regression of } X \text{ on } Y$, and obtained similar results to those reported in the text.

2. Drawing from the conditional distribution $p(\tilde{\mathbf{F}}_T | \tilde{\mathbf{X}}_T, \theta)$

As in Nelson and Kim (p. 191), the conditional distribution of the whole history of factors $p(\tilde{\mathbf{F}}_T | \tilde{\mathbf{X}}_T, \theta)$ can be expressed as the product of conditional distributions of factors at each date t as follows:

$$(A.5) \quad p(\tilde{\mathbf{F}}_T | \tilde{\mathbf{X}}_T, \theta) = p(\mathbf{F}_T | \tilde{\mathbf{X}}_T, \theta) \prod_{t=1}^{T-1} p(\mathbf{F}_t | \mathbf{F}_{t+1}, \tilde{\mathbf{X}}_t, \theta)$$

where $\tilde{\mathbf{X}}_t = (\mathbf{X}_1, \mathbf{X}_2, \dots, \mathbf{X}_t)$. (A.5) relies on the Markov property of \mathbf{F}_t , which implies that $p(\mathbf{F}_t | \mathbf{F}_{t+1}, \mathbf{F}_{t+2}, \dots, \mathbf{F}_T, \mathbf{X}_T, \theta) = p(\mathbf{F}_t | \mathbf{F}_{t+1}, \mathbf{X}_t, \theta)$.

Because the state-space model (A.3)-(A.4) is linear and Gaussian, we have

$$(A.6) \quad \begin{aligned} \mathbf{F}_T | \tilde{\mathbf{X}}_T, \theta &\sim N(\mathbf{F}_{T|T}, \mathbf{P}_{T|T}) \\ \mathbf{F}_t | \mathbf{F}_{t+1}, \tilde{\mathbf{X}}_t, \theta &\sim N(\mathbf{F}_{t|t, \mathbf{F}_{t+1}}, \mathbf{P}_{t|t, \mathbf{F}_{t+1}}) \quad t = T-1, \dots, 1 \end{aligned}$$

where

$$(A.7) \quad \begin{aligned} \mathbf{F}_{T|T} &= E(\mathbf{F}_T | \tilde{\mathbf{X}}_T, \theta) \\ \mathbf{P}_{T|T} &= Cov(\mathbf{F}_T | \tilde{\mathbf{X}}_T, \theta) \\ \mathbf{F}_{t|t, \mathbf{F}_{t+1}} &= E(\mathbf{F}_t | \mathbf{F}_{t+1}, \tilde{\mathbf{X}}_t, \theta) = E(\mathbf{F}_t | \mathbf{F}_{t+1}, \mathbf{F}_{t|t}, \theta) \\ \mathbf{P}_{t|t, \mathbf{F}_{t+1}} &= Cov(\mathbf{F}_t | \mathbf{F}_{t+1}, \tilde{\mathbf{X}}_t, \theta) = Cov(\mathbf{F}_t | \mathbf{F}_{t+1}, \mathbf{F}_{t|t}, \theta) \end{aligned}$$

where the notation $\mathbf{F}_{t|t}$ refers to the expectation of \mathbf{F}_t conditional on information dated t or earlier. To obtain these, we first calculate $\mathbf{F}_{t|t}$ and $\mathbf{P}_{t|t}$, $t = 1, 2, \dots, T$, by Kalman filter, conditional on θ and the data through period t , $\tilde{\mathbf{X}}_t$, with starting values of zeros for the factors and the identity matrix for the covariance matrix (Hamilton, 1994). The last iteration of the filter yields $\mathbf{F}_{T|T}$ and $\mathbf{P}_{T|T}$, which together with the first line of (A.6) allows us to draw a value for \mathbf{F}_T . Treating this drawn value as extra information, we can move “backwards in time” through the sample, using the Kalman filter to obtain updated

values of $\mathbf{F}_{T-1|T-1, \mathbf{F}_T}$ and $\mathbf{P}_{T-1|T-1, \mathbf{F}_T}$; drawing a value of \mathbf{F}_{T-1} using the second line of (A.6); and continuing in similar manner to draw values for \mathbf{F}_t , $t = T-2, T-3, \dots, 1$.

If the order d of $\Phi(L)$ exceeds one, as it does in our applications, then lags of the factors appear in the state vector \mathbf{F}_t and Q is singular, as is $\mathbf{P}_{t|t, \mathbf{F}_{t+1}}$ for any $t < T$. (The singularity of these two covariance matrices follows from the fact that, in this case, \mathbf{F}_t and \mathbf{F}_{t+1} have common components.) In this case we cannot condition on the full vector \mathbf{F}_{t+1} when drawing \mathbf{F}_t , but only on the first d elements of \mathbf{F}_{t+1} . Kim and Nelson (1999, p. 194-6) show how to modify the Kalman filter algorithm in this case.

3. Drawing from the conditional distribution $p(\theta | \tilde{\mathbf{X}}_T, \tilde{\mathbf{F}}_T)$.

Conditional on the observed data and the estimated factors from the previous iteration, a new iteration is begun by drawing a new value of the parameters θ . With known factors, (A.3) and (A.4) amount to standard regression equations, with (A.3) specifying the distribution of Λ and R , and (A.4) the distribution of $\text{vec}(\Phi)$ and Q . Consider (A.3) first. Because the errors are uncorrelated, we can apply OLS to (A.3) equation by equation to obtain $\hat{\Lambda}$ and \hat{e} . We set $R_{ij} = 0$, $i \neq j$ and assume a proper (conjugate) but diffuse Inverse-Gamma (3, 0.001) prior for R_{ii} . Standard Bayesian results (see Bauwens, Lubrano and Richard, 1999, p. 58) deliver posterior of the form:

$$R_{ii} | \tilde{\mathbf{X}}_T, \tilde{\mathbf{F}}_T \sim iG(\bar{R}_{ii}, T + 0.001)$$

where $\bar{R}_{ii} = 3 + \hat{e}_i' \hat{e}_i + \hat{\Lambda}_i' [M_0^{-1} + (\tilde{\mathbf{F}}_T^{(i)'} \tilde{\mathbf{F}}_T^{(i)})^{-1}]^{-1} \hat{\Lambda}_i$. Here M_0^{-1} denotes variance parameter in the prior on the coefficients of the i -th equation, Λ_i , which, conditional on the drawn

value of R_{ii} , is $N(0, R_{ii}M_0^{-1})$. We set $M_0 = I$. $\tilde{\mathbf{F}}_T^{(i)}$ corresponds to the regressors of the i -th equation. We draw values for Λ_i from the posterior $N(\bar{\Lambda}_i, R_{ii}\bar{M}_i^{-1})$, where

$$\bar{\Lambda}_i = \bar{M}_i^{-1}(\tilde{\mathbf{F}}_T^{(i)'}\tilde{\mathbf{F}}_T^{(i)})\hat{\Lambda}_i \text{ and } \bar{M}_i = M_0 + \tilde{\mathbf{F}}_T^{(i)'}\tilde{\mathbf{F}}_T^{(i)}.$$

Turning to (A.4), we see that this system has a standard VAR form and can thus also be estimated equation by equation, to obtain $vec(\hat{\Phi}), \hat{Q}$. Proceeding similarly as before, we impose a diffuse conjugate Normal-Wishart prior,

$$vec(\Phi) | Q \sim N(0, Q \otimes \Omega_0), Q \sim iW(Q_0, K + M + 2),$$

where $vec(\Phi)$ is the rows of Φ stacked in a column vector of length $d(K + M)^2$. We choose its parameters so as to express the belief that parameters on longer lags are more likely to be zero, in the spirit of the Minnesota prior. Following Kadiyala and Karlsson (1997) we set the diagonal elements of Q_0 to the residual variances of the corresponding d -lag univariate autoregressions, $\hat{\sigma}_i^2$. To match prior variances of the Minnesota prior we construct diagonal elements of Ω_0 so that the prior variance of parameter on k lagged j 'th variable in i 'th equation equals $\sigma_i^2 / k\sigma_j^2$. We start by drawing Q from the Inverse-Wishart, $iW(\bar{Q}, T + K + M + 2)$, where $\bar{Q} = Q_0 + \hat{V}'\hat{V} + \hat{\Phi}'[\Omega_0 + (\tilde{\mathbf{F}}_{T-1}'\tilde{\mathbf{F}}_{T-1})^{-1}]^{-1}\hat{\Phi}$ and \hat{V} is the matrix of OLS residuals. Conditional on the sampled Q , we then draw $\{\Phi^{ijt}\}$ from the conditional normal according to

$$vec(\Phi) \sim N(vec(\bar{\Phi}), Q \otimes \bar{\Omega})$$

where $\bar{\Phi} = \bar{\Omega}(\tilde{\mathbf{F}}_{T-1}'\tilde{\mathbf{F}}_{T-1})\hat{\Phi}$ and $\bar{\Omega} = (\Omega_0^{-1} + \tilde{\mathbf{F}}_{T-1}'\tilde{\mathbf{F}}_{T-1})^{-1}$. Stationarity is enforced by discarding draws of Φ that contain roots greater than or equal to 1.001 in absolute value.

This completes the sampling of the parameters θ conditional on the estimated factors from the previous iteration and the observed data.

Steps 2 and 3 are repeated for each iteration s . Inference is based on the distribution of $(\tilde{\mathbf{F}}_T^s, \theta^s)$, for $s \geq B$, with B large enough to guarantee convergence of the algorithm. As noted, the empirical distribution from the sampling procedure should well approximate the joint posterior or normalized joint likelihood. Calculating medians and quantiles of $(\tilde{\mathbf{F}}_T^s, \theta^s)$ for $s = B, \dots, S$ provides estimates of the values of the factors and the model parameters and the associated confidence regions. Note that the Gibbs-sampling algorithm is guaranteed to closely approximate the shape of the likelihood, especially around its peak, even if the likelihood is rather irregular and complicated, as is typically the case in the large models considered in this paper.

Appendix B - Data Description

All series were directly taken from DRI/McGraw Hill Basic Economics Database. Format is as in Stock & Watson's papers: series number; series mnemonic; data span; transformation code and series description as appears in the database. The transformation codes are: 1 – no transformation; 2 – first difference; 4 – logarithm; 5 – first difference of logarithm. An asterisk, '*', next to the mnemonic denotes a variable assumed to be "slow-moving" in the estimation.

Real output and income

1.	IPP*	1959:01-2001:08	5 INDUSTRIAL PRODUCTION: PRODUCTS, TOTAL (1992=100,SA)
2.	IPF*	1959:01-2001:08	5 INDUSTRIAL PRODUCTION: FINAL PRODUCTS (1992=100,SA)
3.	IPC*	1959:01-2001:08	5 INDUSTRIAL PRODUCTION: CONSUMER GOODS (1992=100,SA)
4.	IPCD*	1959:01-2001:08	5 INDUSTRIAL PRODUCTION: DURABLE CONS. GOODS (1992=100,SA)
5.	IPCN*	1959:01-2001:08	5 INDUSTRIAL PRODUCTION: NONDURABLE CONS. GOODS (1992=100,SA)
6.	IPE*	1959:01-2001:08	5 INDUSTRIAL PRODUCTION: BUSINESS EQUIPMENT (1992=100,SA)
7.	IPI*	1959:01-2001:08	5 INDUSTRIAL PRODUCTION: INTERMEDIATE PRODUCTS (1992=100,SA)
8.	IPM*	1959:01-2001:08	5 INDUSTRIAL PRODUCTION: MATERIALS (1992=100,SA)
9.	IPMD*	1959:01-2001:08	5 INDUSTRIAL PRODUCTION: DURABLE GOODS MATERIALS (1992=100,SA)
10.	IPMND*	1959:01-2001:08	5 INDUSTRIAL PRODUCTION: NONDUR. GOODS MATERIALS (1992=100,SA)
11.	IPMFG*	1959:01-2001:08	5 INDUSTRIAL PRODUCTION: MANUFACTURING (1992=100,SA)
12.	IPD*	1959:01-2001:08	5 INDUSTRIAL PRODUCTION: DURABLE MANUFACTURING (1992=100,SA)
13.	IPN*	1959:01-2001:08	5 INDUSTRIAL PRODUCTION: NONDUR. MANUFACTURING (1992=100,SA)
14.	IPMIN*	1959:01-2001:08	5 INDUSTRIAL PRODUCTION: MINING (1992=100,SA)
15.	IPUT*	1959:01-2001:08	5 INDUSTRIAL PRODUCTION: UTILITIES (1992=100,SA)
16.	IP*	1959:01-2001:08	5 INDUSTRIAL PRODUCTION: TOTAL INDEX (1992=100,SA)
17.	IPXMCA*	1959:01-2001:08	1 CAPACITY UTIL RATE: MANUFAC.,TOTAL(% OF CAPACITY,SA)(FRB)
18.	PMI*	1959:01-2001:08	1 PURCHASING MANAGERS' INDEX (SA)
19.	PMP*	1959:01-2001:08	1 NAPM PRODUCTION INDEX (PERCENT)
20.	GMPYQ*	1959:01-2001:08	5 PERSONAL INCOME (CHAINED) (SERIES #52) (BIL 92\$,SAAR)
21.	GMYPQ*	1959:01-2001:08	5 PERSONAL INC. LESS TRANS. PAYMENTS (CHAINED) (#51) (BIL 92\$,SAAR)

Employment and hours

22.	LHEL*	1959:01-2001:08	5 INDEX OF HELP-WANTED ADVERTISING IN NEWSPAPERS (1967=100;SA)
23.	LHELX*	1959:01-2001:08	4 EMPLOYMENT: RATIO; HELP-WANTED ADS:NO. UNEMPLOYED CLF
24.	LHEM*	1959:01-2001:08	5 CIVILIAN LABOR FORCE: EMPLOYED, TOTAL (THOUS.,SA)
25.	LHNAG*	1959:01-2001:08	5 CIVILIAN LABOR FORCE: EMPLOYED, NONAG.INDUSTRIES (THOUS.,SA)
26.	LHUR*	1959:01-2001:08	1 UNEMPLOYMENT RATE: ALL WORKERS, 16 YEARS & OVER (%;SA)
27.	LHU680*	1959:01-2001:08	1 UNEMPLOY.BY DURATION: AVERAGE(MEAN)DURATION IN WEEKS (SA)
28.	LHU5*	1959:01-2001:08	1 UNEMPLOY.BY DURATION: PERS UNEMPL.LESS THAN 5 WKS (THOUS.,SA)
29.	LHU14*	1959:01-2001:08	1 UNEMPLOY.BY DURATION: PERS UNEMPL.5 TO 14 WKS (THOUS.,SA)
30.	LHU15*	1959:01-2001:08	1 UNEMPLOY.BY DURATION: PERS UNEMPL.15 WKS + (THOUS.,SA)
31.	LHU26*	1959:01-2001:08	1 UNEMPLOY.BY DURATION: PERS UNEMPL.15 TO 26 WKS (THOUS.,SA)
32.	LPNAG*	1959:01-2001:08	5 EMPLOYEES ON NONAG. PAYROLLS: TOTAL (THOUS.,SA)
33.	LP*	1959:01-2001:08	5 EMPLOYEES ON NONAG PAYROLLS: TOTAL, PRIVATE (THOUS,SA)
34.	LPGD*	1959:01-2001:08	5 EMPLOYEES ON NONAG. PAYROLLS: GOODS-PRODUCING (THOUS.,SA)
35.	LPMI*	1959:01-2001:08	5 EMPLOYEES ON NONAG. PAYROLLS: MINING (THOUS.,SA)
36.	LPCC*	1959:01-2001:08	5 EMPLOYEES ON NONAG. PAYROLLS: CONTRACT CONSTRUC. (THOUS.,SA)
37.	LPEM*	1959:01-2001:08	5 EMPLOYEES ON NONAG. PAYROLLS: MANUFACTURING (THOUS.,SA)
38.	LPED*	1959:01-2001:08	5 EMPLOYEES ON NONAG. PAYROLLS: DURABLE GOODS (THOUS.,SA)
39.	LPEN*	1959:01-2001:08	5 EMPLOYEES ON NONAG. PAYROLLS: NONDURABLE GOODS (THOUS.,SA)
40.	LPSP*	1959:01-2001:08	5 EMPLOYEES ON NONAG. PAYROLLS: SERVICE-PRODUCING (THOUS.,SA)
41.	LPTU*	1959:01-2001:08	5 EMPLOYEES ON NONAG. PAYROLLS: TRANS. & PUBLIC UTIL. (THOUS.,SA)
42.	LPT*	1959:01-2001:08	5 EMPLOYEES ON NONAG. PAYROLLS: WHOLESALE & RETAIL (THOUS.,SA)
43.	LPFR*	1959:01-2001:08	5 EMPLOYEES ON NONAG. PAYROLLS: FINANCE,INS.&REAL EST (THOUS.,SA)
44.	LPS*	1959:01-2001:08	5 EMPLOYEES ON NONAG. PAYROLLS: SERVICES (THOUS.,SA)
45.	LPGOV*	1959:01-2001:08	5 EMPLOYEES ON NONAG. PAYROLLS: GOVERNMENT (THOUS.,SA)
46.	LPHRM*	1959:01-2001:08	1 AVG. WEEKLY HRS. OF PRODUCTION WKRS.: MANUFACTURING (SA)

47. LPMOSA*	1959:01-2001:08	1 AVG. WEEKLY HRS. OF PROD. WKRS.: MFG.,OVERTIME HRS. (SA)
48. PMEMP*	1959:01-2001:08	1 NAPM EMPLOYMENT INDEX (PERCENT)

Consumption

49. GMCQ*	1959:01-2001:08	5 PERSONAL CONSUMPTION EXPEND (CHAINED) - TOTAL (BIL 92\$,SAAR)
50. GMCDQ*	1959:01-2001:08	5 PERSONAL CONSUMPTION EXPEND (CHAINED) – TOT. DUR. (BIL 96\$,SAAR)
51. GMCNQ*	1959:01-2001:08	5 PERSONAL CONSUMPTION EXPEND (CHAINED) – NONDUR. (BIL 92\$,SAAR)
52. GMCSQ*	1959:01-2001:08	5 PERSONAL CONSUMPTION EXPEND (CHAINED) - SERVICES (BIL 92\$,SAAR)
53. GMCANQ*	1959:01-2001:08	5 PERSONAL CONS EXPEND (CHAINED) - NEW CARS (BIL 96\$,SAAR)

Housing starts and sales

54. HSFR	1959:01-2001:08	4 HOUSING STARTS:NONFARM(1947-58);TOT.(1959-)(THOUS.,SA
55. HSNE	1959:01-2001:08	4 HOUSING STARTS:NORTHEAST (THOUS.U.)S.A.
56. HSMW	1959:01-2001:08	4 HOUSING STARTS:MIDWEST(THOUS.U.)S.A.
57. HSSOU	1959:01-2001:08	4 HOUSING STARTS:SOUTH (THOUS.U.)S.A.
58. HSWST	1959:01-2001:08	4 HOUSING STARTS:WEST (THOUS.U.)S.A.
59. HSBR	1959:01-2001:08	4 HOUSING AUTHORIZED: TOTAL NEW PRIV HOUSING (THOUS.,SAAR)
60. HMOB	1959:01-2001:08	4 MOBILE HOMES: MANUFACTURERS' SHIPMENTS (THOUS.OF UNITS,SAAR)

Real inventories, orders and unfilled orders

61. PMNV	1959:01-2001:08	1 NAPM INVENTORIES INDEX (PERCENT)
62. PMNO	1959:01-2001:08	1 NAPM NEW ORDERS INDEX (PERCENT)
63. PMDEL	1959:01-2001:08	1 NAPM VENDOR DELIVERIES INDEX (PERCENT)
64. MOCMQ	1959:01-2001:08	5 NEW ORDERS (NET) - CONSUMER GOODS & MATERIALS, 1992 \$ (BCI)
65. MSONDQ	1959:01-2001:08	5 NEW ORDERS, NONDEFENSE CAPITAL GOODS, IN 1992 DOLLARS (BCI)

Stock prices

66. FSNCOM	1959:01-2001:08	5 NYSE COMMON STOCK PRICE INDEX: COMPOSITE (12/31/65=50)
67. FSPCOM	1959:01-2001:08	5 S&P'S COMMON STOCK PRICE INDEX: COMPOSITE (1941-43=10)
68. FSPIN	1959:01-2001:08	5 S&P'S COMMON STOCK PRICE INDEX: INDUSTRIALS (1941-43=10)
69. FSPCAP	1959:01-2001:08	5 S&P'S COMMON STOCK PRICE INDEX: CAPITAL GOODS (1941-43=10)
70. FSPUT	1959:01-2001:08	5 S&P'S COMMON STOCK PRICE INDEX: UTILITIES (1941-43=10)
71. FSDXP	1959:01-2001:08	1 S&P'S COMPOSITE COMMON STOCK: DIVIDEND YIELD (% PER ANNUM)
72. FSPXE	1959:01-2001:08	1 S&P'S COMPOSITE COMMON STOCK: PRICE-EARNINGS RATIO (%NSA)

Exchange rates

73. EXRSW	1959:01-2001:08	5 FOREIGN EXCHANGE RATE: SWITZERLAND (SWISS FRANC PER U.S.\$)
74. EXRJAN	1959:01-2001:08	5 FOREIGN EXCHANGE RATE: JAPAN (YEN PER U.S.\$)
75. EXRUK	1959:01-2001:08	5 FOREIGN EXCHANGE RATE: UNITED KINGDOM (CENTS PER POUND)
76. EXRCAN	1959:01-2001:08	5 FOREIGN EXCHANGE RATE: CANADA (CANADIAN \$ PER U.S.\$)

Interest rates

77. FYFF	1959:01-2001:08	1 INTEREST RATE: FEDERAL FUNDS (EFFECTIVE) (% PER ANNUM,NSA)
78. FYGM3	1959:01-2001:08	1 INTEREST RATE: U.S.TREASURY BILLS,SEC MKT,3-MO.(% PER ANN,NSA)
79. FYGM6	1959:01-2001:08	1 INTEREST RATE: U.S.TREASURY BILLS,SEC MKT,6-MO.(% PER ANN,NSA)
80. FYGT1	1959:01-2001:08	1 INTEREST RATE: U.S.TREASURY CONST MATUR. ,1-YR.(% PER ANN,NSA)

81. FYGT5	1959:01-2001:08	1 INTEREST RATE: U.S.TREASURY CONST MATUR., 5-YR.(% PER ANN,NSA)
82. FYGT10	1959:01-2001:08	1 INTEREST RATE: U.S.TREASURY CONST MATUR.,10-YR.(% PER ANN,NSA)
83. FYAAAC	1959:01-2001:08	1 BOND YIELD: MOODY'S AAA CORPORATE (% PER ANNUM)
84. FYBAAC	1959:01-2001:08	1 BOND YIELD: MOODY'S BAA CORPORATE (% PER ANNUM)
85. SFYGM3	1959:01-2001:08	1 Spread FYGM3 - FYFF
86. SFYGM6	1959:01-2001:08	1 Spread FYGM6 - FYFF
87. SFYGT1	1959:01-2001:08	1 Spread FYGT1 - FYFF
88. SFYGT5	1959:01-2001:08	1 Spread FYGT5 - FYFF
89. SFYGT10	1959:01-2001:08	1 Spread FYGT10 - FYFF
90. SFYAAAC	1959:01-2001:08	1 Spread FYAAAC - FYFF
91. SFYBAAC	1959:01-2001:08	1 Spread FYBAAC - FYFF

Money and credit quantity aggregates

92. FM1	1959:01-2001:08	5 MONEY STOCK: M1 (BIL\$,SA)
93. FM2	1959:01-2001:08	5 MONEY STOCK:M2 (BIL\$, SA)
94. FM3	1959:01-2001:08	5 MONEY STOCK: M3 (BIL\$,SA)
95. FM2DQ	1959:01-2001:08	5 MONEY SUPPLY - M2 IN 1992 DOLLARS (BCI)
96. FMFBA	1959:01-2001:08	5 MONETARY BASE, ADJ FOR RESERVE REQUIREMENT CHANGES(MIL\$,SA)
97. FMRRRA	1959:01-2001:08	5 DEPOSITORY INST RESERVES:TOTAL,ADJ FOR RES. REQ CHGS(MIL\$,SA)
98. FMRNBA	1959:01-2001:08	5 DEPOSITORY INST RESERVES:NONBOR. ,ADJ RES REQ CHGS(MIL\$,SA)
99. FCLNQ	1959:01-2001:08	5 COMMERCIAL & INDUST. LOANS OUSTANDING IN 1992 DOLLARS (BCI)
100. FCLBMC	1959:01-2001:08	1 WKLY RP LG COM. BANKS: NET CHANGE COM & IND. LOANS(BIL\$,SAAR)
101. CCINRV	1959:01-2001:08	5 CONSUMER CREDIT OUTSTANDING NONREVOLVING G19

Price indexes

102. PMCP	1959:01-2001:08	1 NAPM COMMODITY PRICES INDEX (PERCENT)
103. PWFSA*	1959:01-2001:08	5 PRODUCER PRICE INDEX: FINISHED GOODS (82=100,SA)
104. PWFCSA*	1959:01-2001:08	5 PRODUCER PRICE INDEX:FINISHED CONSUMER GOODS (82=100,SA)
105. PWIMSA*	1959:01-2001:08	5 PRODUCER PRICE INDEX:INTERMED MAT.SUP & COMPONENTS(82=100,SA)
106. PWCMSA*	1959:01-2001:08	5 PRODUCER PRICE INDEX:CRUDE MATERIALS (82=100,SA)
107. PSM99Q*	1959:01-2001:08	5 INDEX OF SENSITIVE MATERIALS PRICES (1990=100)(BCI-99A)
108. PUNEW*	1959:01-2001:08	5 CPI-U: ALL ITEMS (82-84=100,SA)
109. PU83*	1959:01-2001:08	5 CPI-U: APPAREL & UPKEEP (82-84=100,SA)
110. PU84*	1959:01-2001:08	5 CPI-U: TRANSPORTATION (82-84=100,SA)
111. PU85*	1959:01-2001:08	5 CPI-U: MEDICAL CARE (82-84=100,SA)
112. PUC*	1959:01-2001:08	5 CPI-U: COMMODITIES (82-84=100,SA)
113. PUCD*	1959:01-2001:08	5 CPI-U: DURABLES (82-84=100,SA)
114. PUS*	1959:01-2001:08	5 CPI-U: SERVICES (82-84=100,SA)
115. PUXF*	1959:01-2001:08	5 CPI-U: ALL ITEMS LESS FOOD (82-84=100,SA)
116. PUXHS*	1959:01-2001:08	5 CPI-U: ALL ITEMS LESS SHELTER (82-84=100,SA)
117. PUXM*	1959:01-2001:08	5 CPI-U: ALL ITEMS LESS MIDICAL CARE (82-84=100,SA)

Average hourly earnings

118. LEHCC*	1959:01-2001:08	5 AVG HR EARNINGS OF CONSTR WKRS: CONSTRUCTION (\$,SA)
119. LEHM*	1959:01-2001:08	5 AVG HR EARNINGS OF PROD WKRS: MANUFACTURING (\$,SA)

Miscellaneous

120. HHSNTN	1959:01-2001:08	1 U. OF MICH. INDEX OF CONSUMER EXPECTATIONS(BCD-83)□
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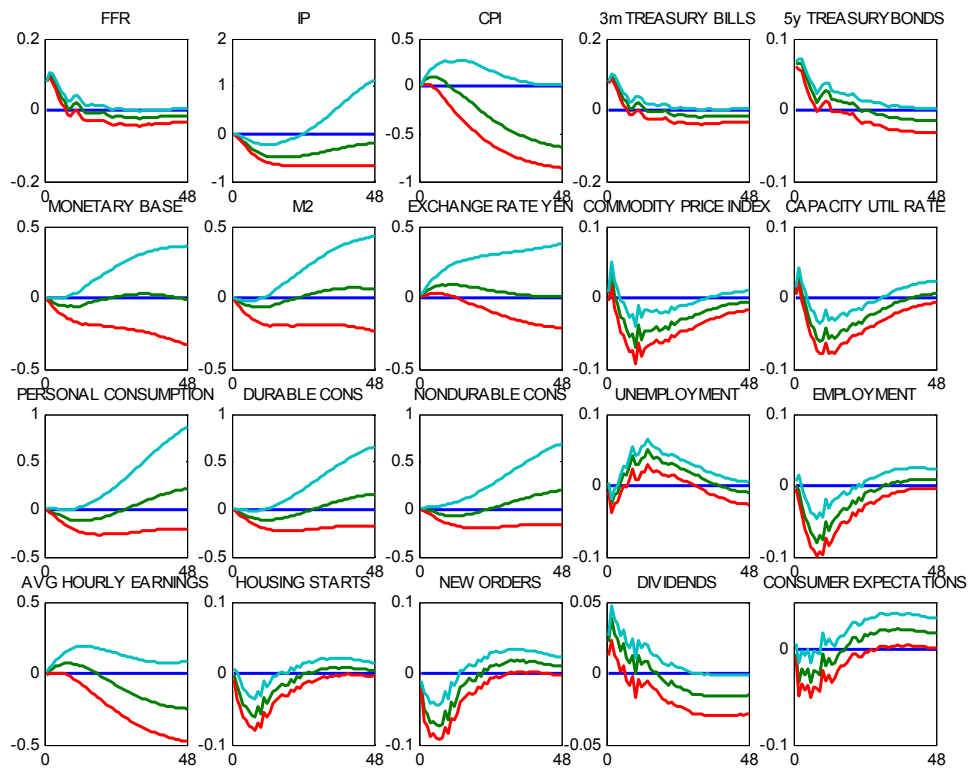


Figure 1. Impulse responses generated from FAVAR with 3 factors and FFR estimated by principal components with 2 step bootstrap.

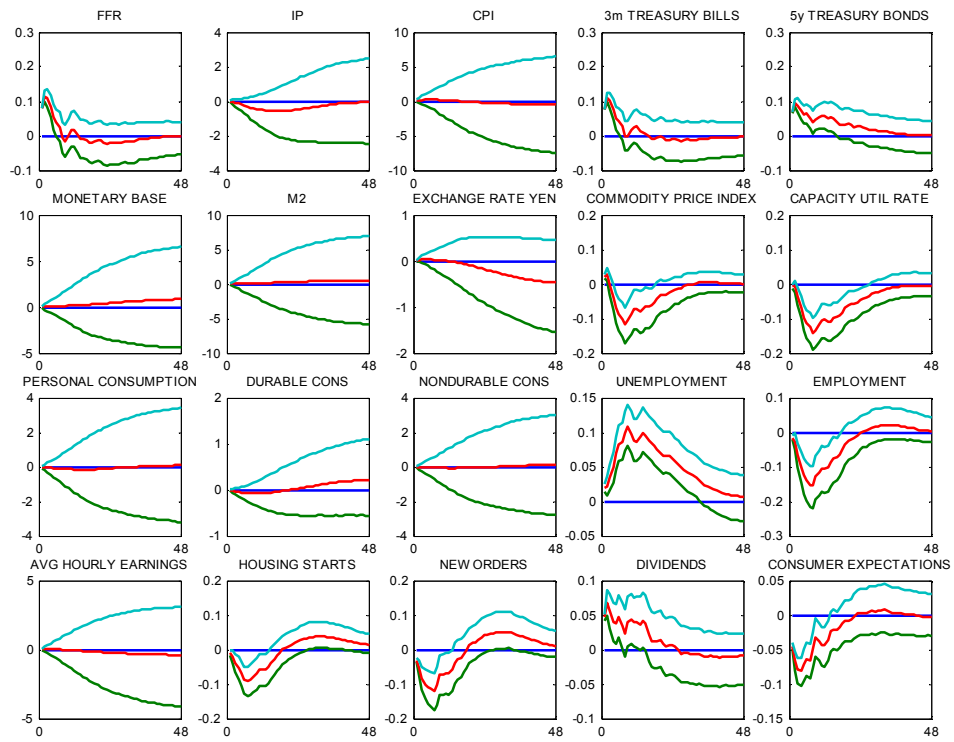


Figure 2. Impulse responses generated from FAVAR with 3 factors and FFR estimated by Gibbs sampling.

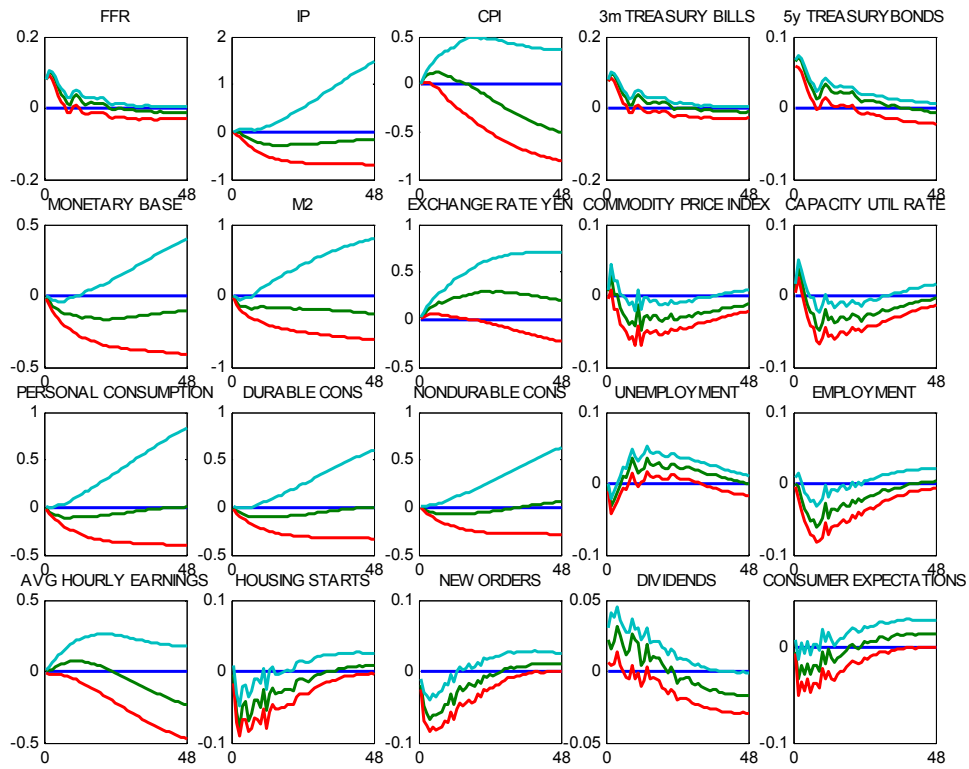


Figure 3. Impulse responses generated from FAVAR with 5 factors and FFR estimated by principal components with 2 step bootstrap.

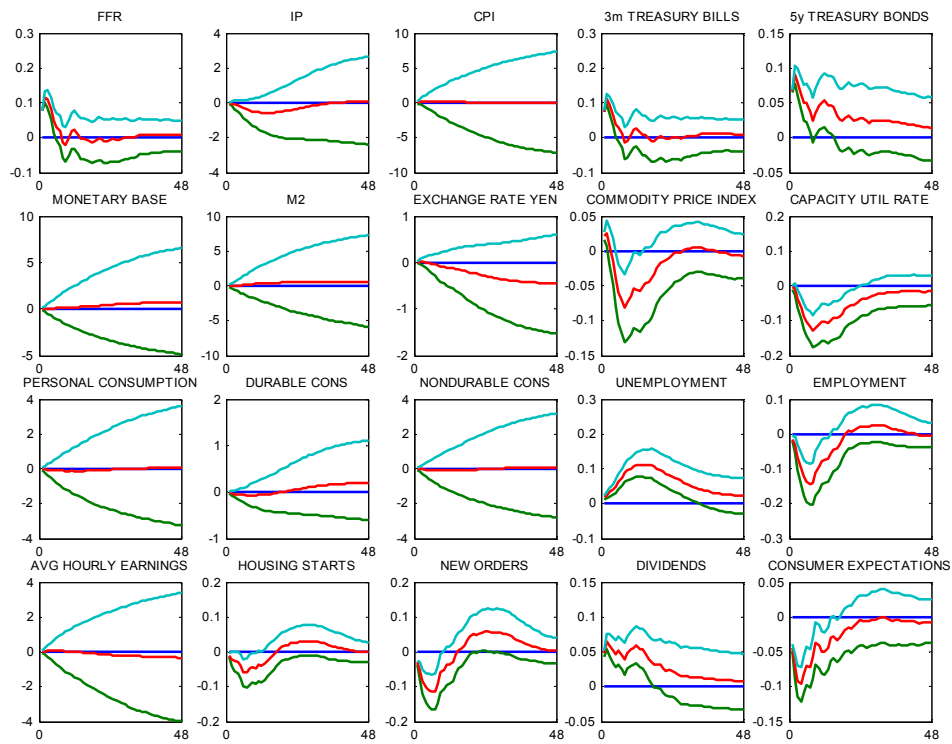


Figure 4. Impulse responses generated from FAVAR with 5 factors and FFR estimated by Gibbs sampling.

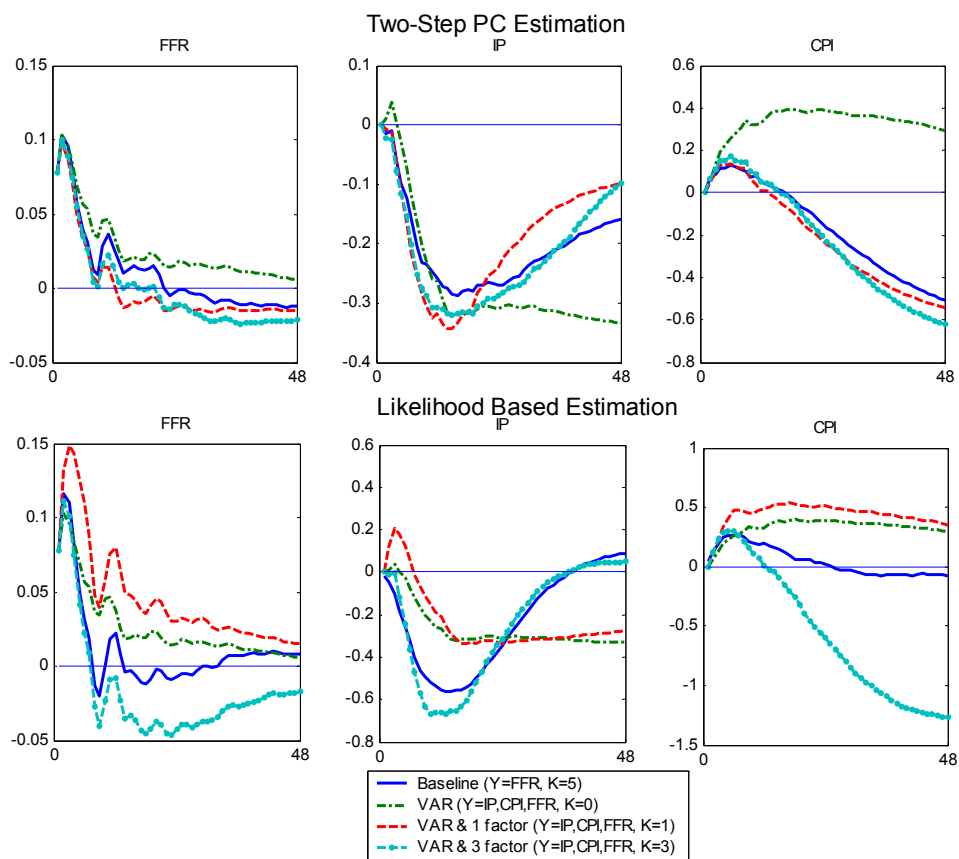


Figure 5. VAR – FAVAR comparison. The top panel displays estimated responses for the two-step principal component estimation and the bottom panel for the likelihood based estimation.

Table 1. Contribution of the policy shock to variance of the common component

Variables	Variance Decomposition	R²
Federal funds rate	0.4538	*1.0000
Industrial production	0.0763	0.7074
Consumer price index	0.0441	0.8699
3-month treasury bill	0.4440	0.9751
5-year bond	0.4354	0.9250
Monetary Base	0.0500	0.1039
M2	0.1035	0.0518
Exchange rate (Yen/\$)	0.2816	0.0252
Commodity price Index	0.0750	0.6518
Capacity utilization	0.1328	0.7533
Personal consumption	0.0535	0.1076
Durable consumption	0.0850	0.0616
Non-durable cons.	0.0327	0.0621
Unemployment	0.1263	0.8168
Employment	0.0934	0.7073
Aver. Hourly Earnings	0.0965	0.0721
Housing Starts	0.0816	0.3872
New Orders	0.1291	0.6236
S&P dividend yield	0.1136	0.5486
Consumer Expectations	0.0514	0.7005

The column entitled “Variance Decomposition” reports the fraction of the variance of the forecast error of the common component, at the 60-month horizon, explained by the policy shock. “R²” refers to the fraction of the variance of the variable explained by the common factors, (\hat{F}_t, Y_t) . See text for details.

*This is by construction.

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